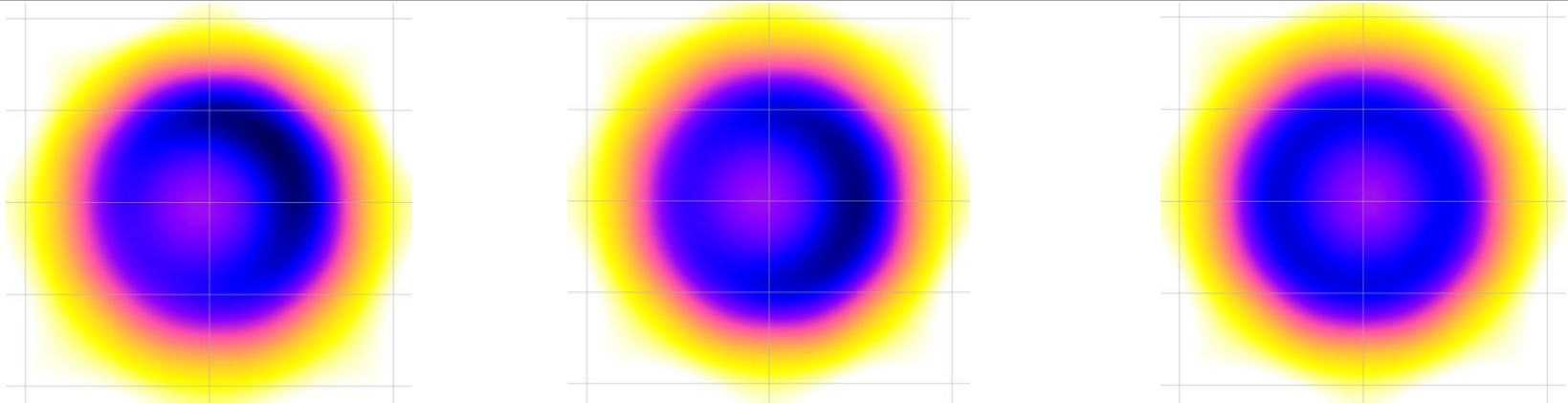


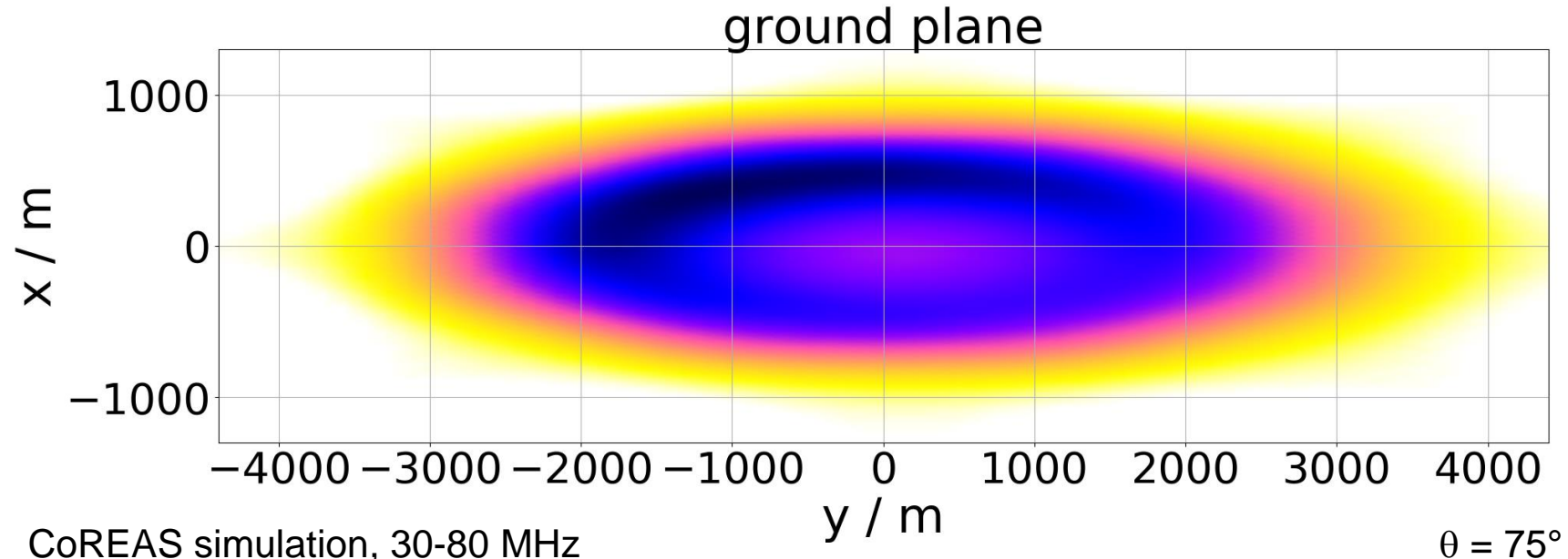
Symmetrizing the signal distribution of radio emission from inclined air showers

Tim Huege (KIT & VUB), Felix Schlüter (KIT) and Lukas Brenk (KIT)



The radio signal distribution of inclined showers

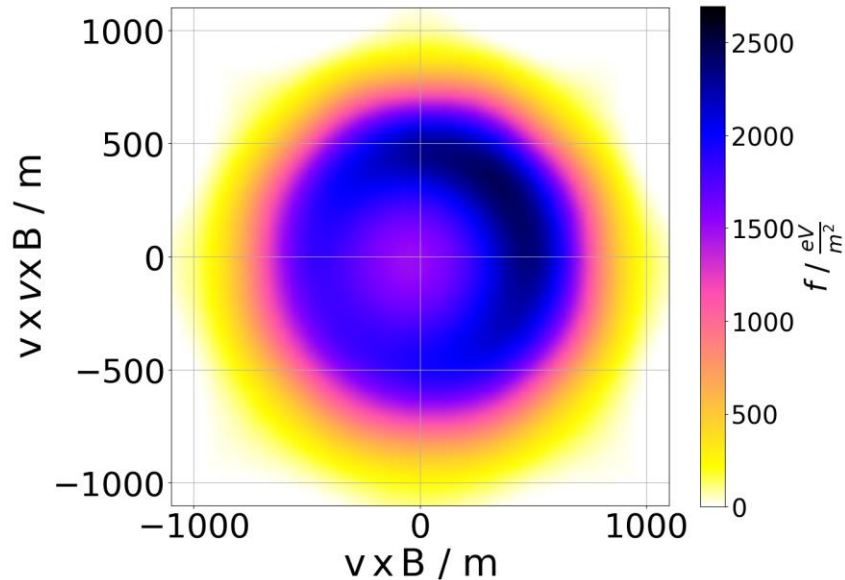
- inclined air showers illuminate elliptical area on the ground
- strong asymmetries in the distribution: geometrical, charge excess



Symmetrizing the signal distribution

- goal: take out asymmetries, then apply simple 1d model LDF

1: raw shower plane

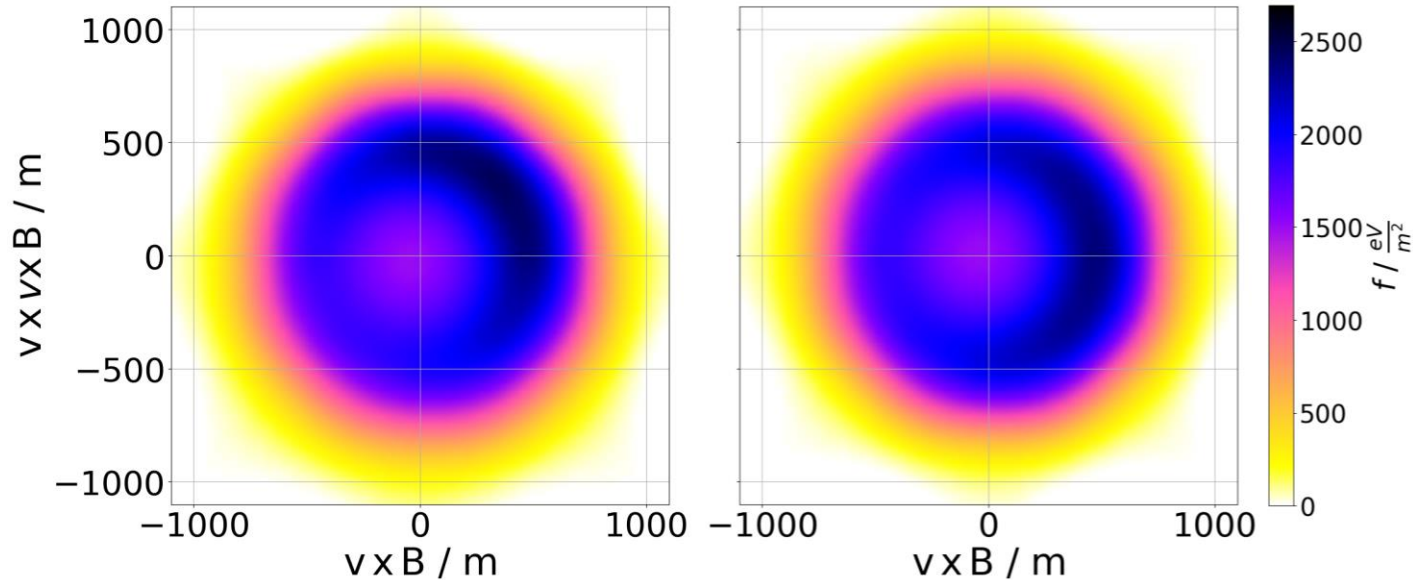


Symmetrizing the signal distribution

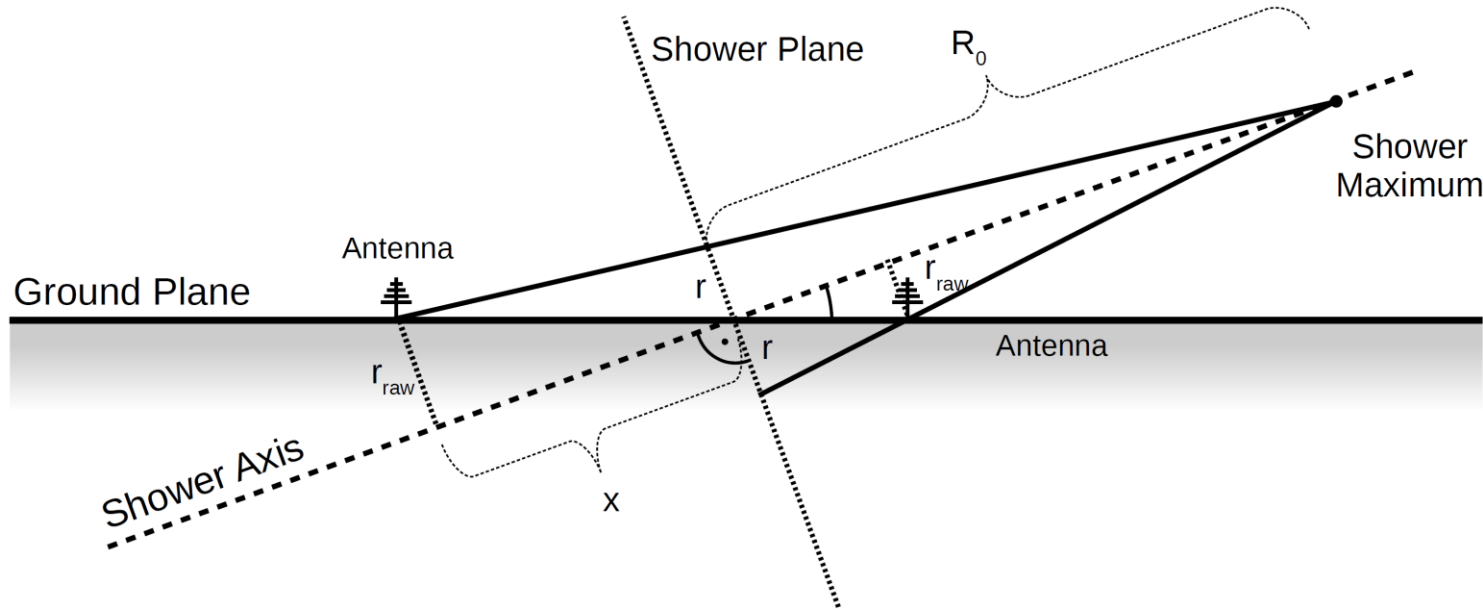
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1: raw shower plane

2: early-late-corrected



Correcting for early-late asymmetries



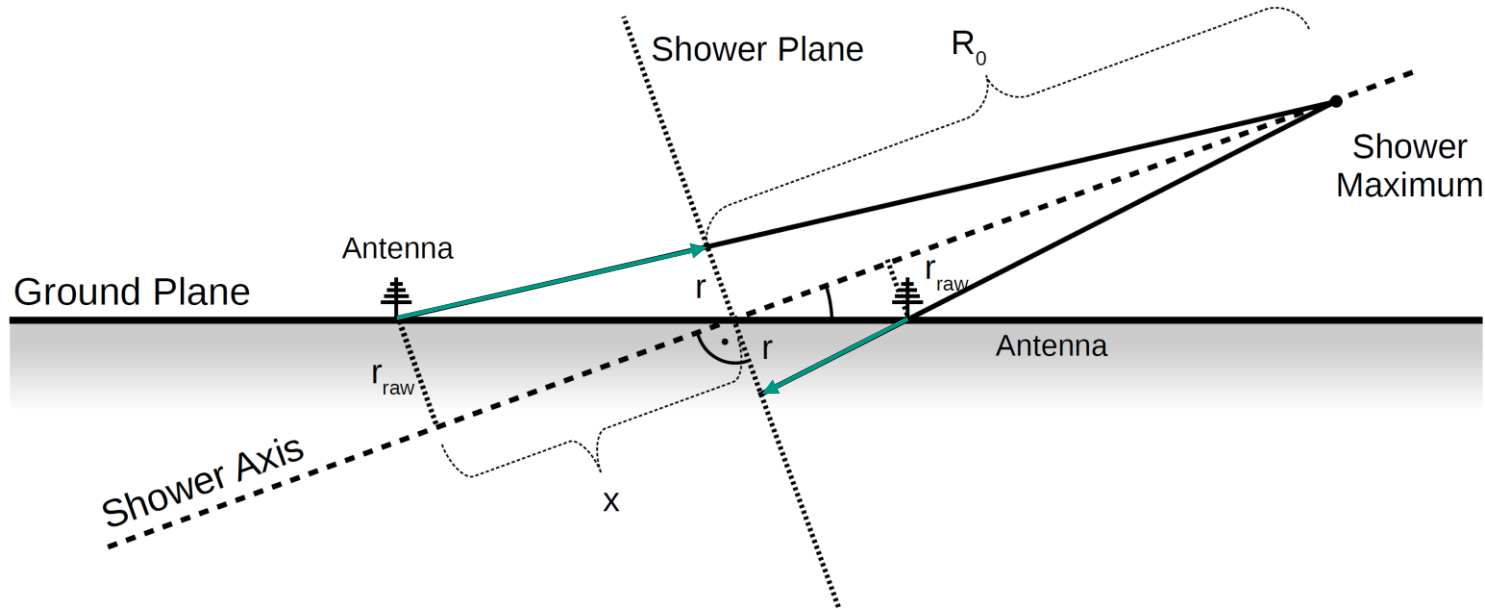
- correcting axis distances and energy fluences

$$f = f_{\text{raw}} \cdot \left(\frac{R}{R_0} \right)^2$$

$$r = r_{\text{raw}} \cdot \frac{R_0}{R}$$

$$R \equiv R_0 + x$$

Correcting for early-late asymmetries



- correcting axis distances and energy fluences

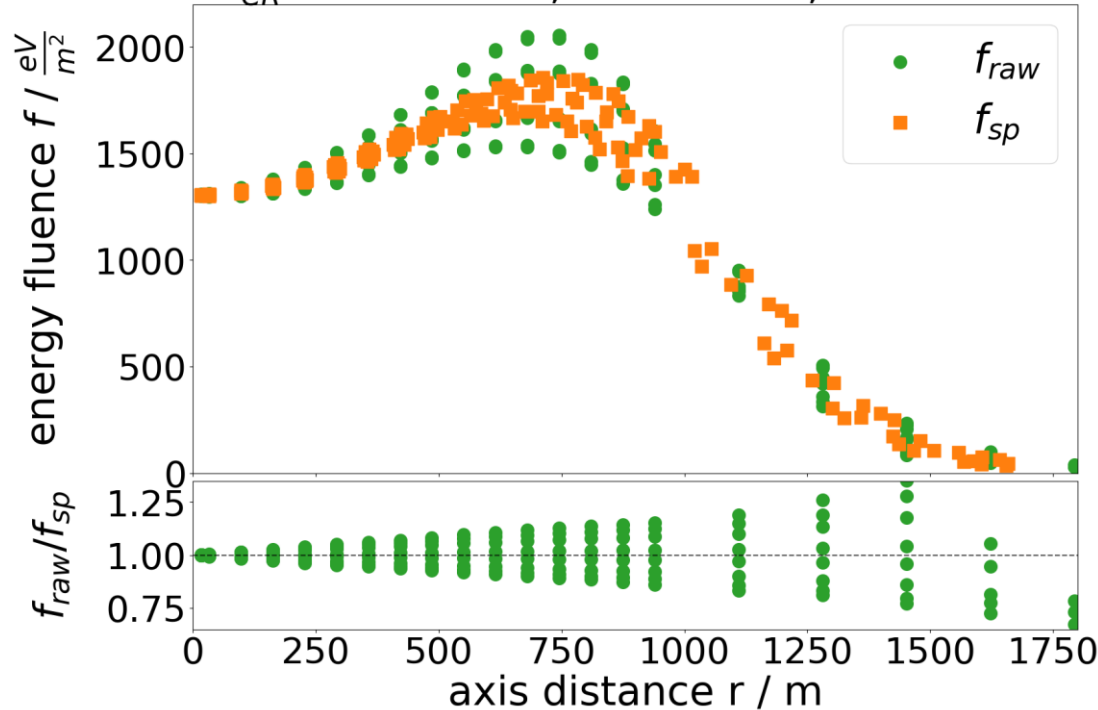
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Performance of early-late correction

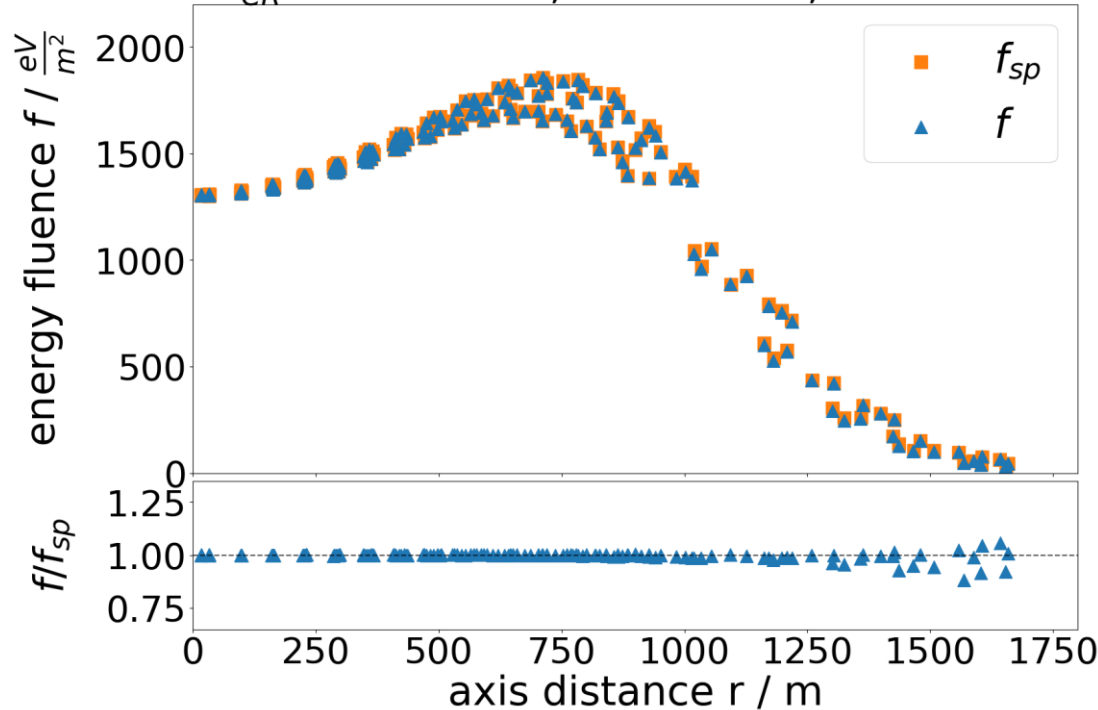
$$E_{CR} = 15.85 \text{ EeV}, \theta = 80.00^\circ, \alpha = 84.15^\circ$$



- compare early-late corrected simulations with direct shower-plane sim.
- correction generally accurate to within 2%
- deviations possibly related to refractive index asymmetries?
(see talk M. Gottowik)

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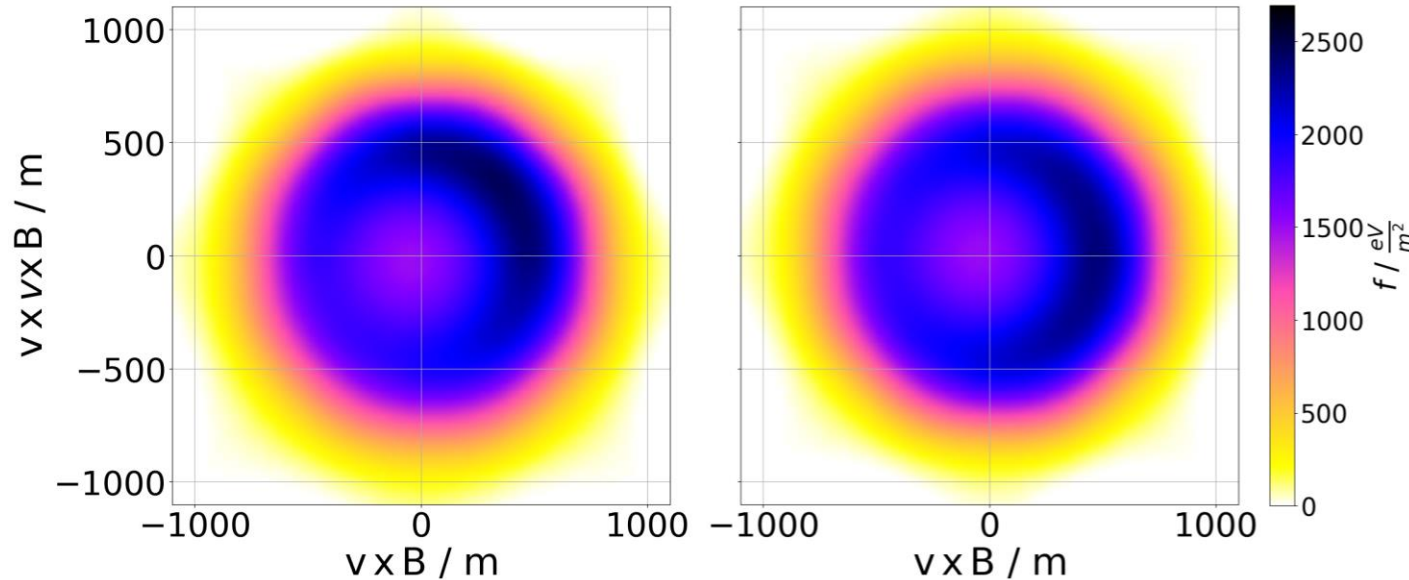
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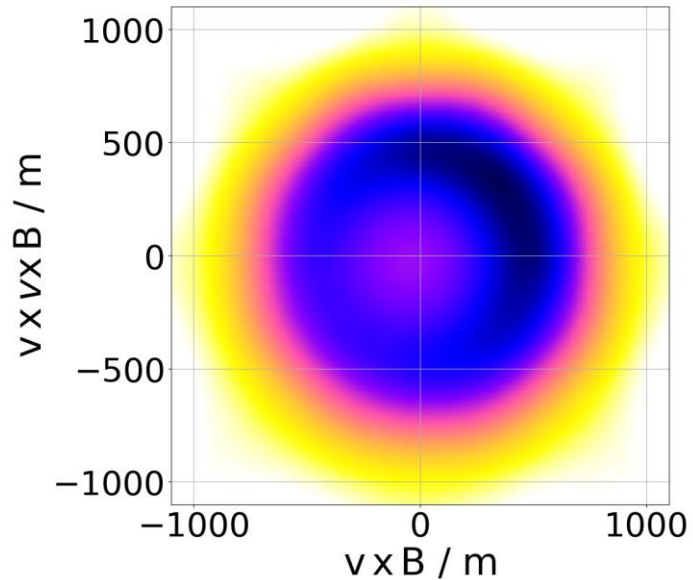
2: early-late-corrected



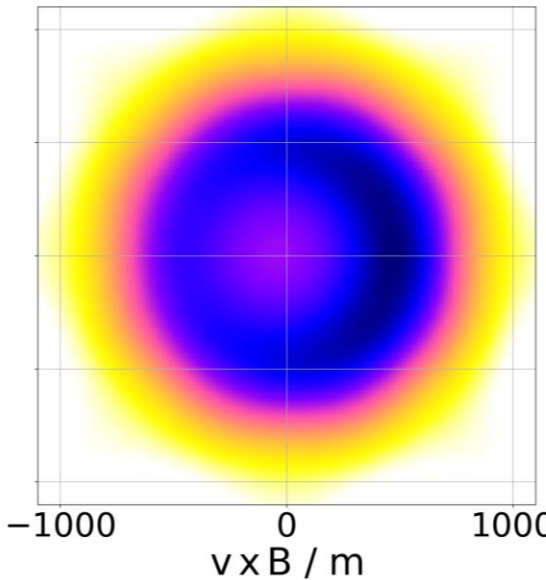
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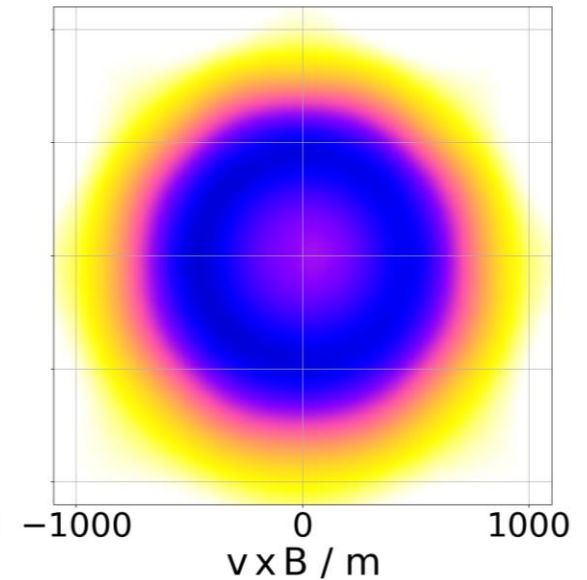
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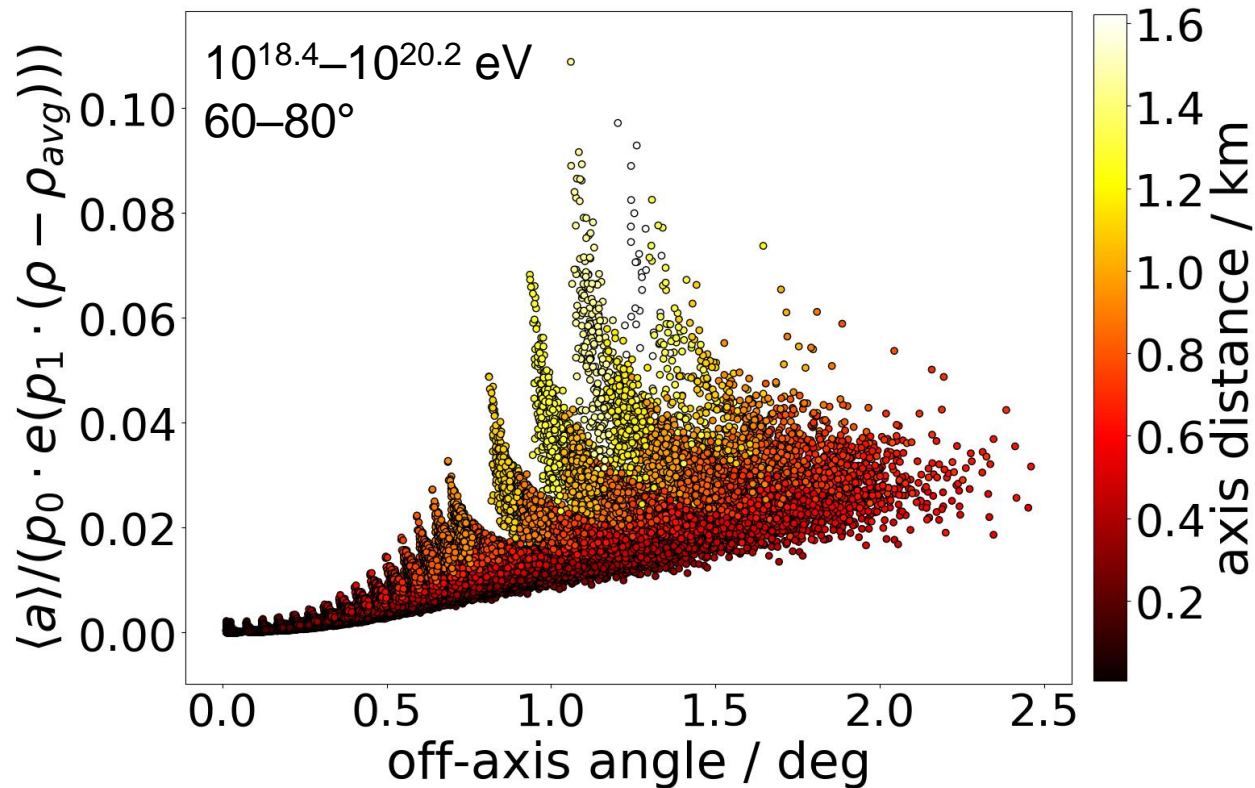
2: early-late-corrected



3: CE subtracted



The charge-excess fraction in the energy fluence



■ charge-excess fraction

$$a \equiv \sin^2(\alpha) \cdot \frac{f_{ce}}{f_{geo}}$$

depends on off-axis angle, lateral distance and density at Xmax

Parameterisation of charge-excess fraction

- analytic parameterization optimized for universal applicability

$$a(r, d_{\max}, \rho_{\max}) = 0.373 \cdot \frac{r}{d_{\max}} \cdot \exp\left(\frac{r}{762.6 \text{ m}}\right) \cdot \left[\exp\left(\frac{\rho_{\max} - \langle \rho_{\max} \rangle}{0.149 \text{ kg/m}^3}\right) - 0.189\right]$$

off-axis angle

axis distance

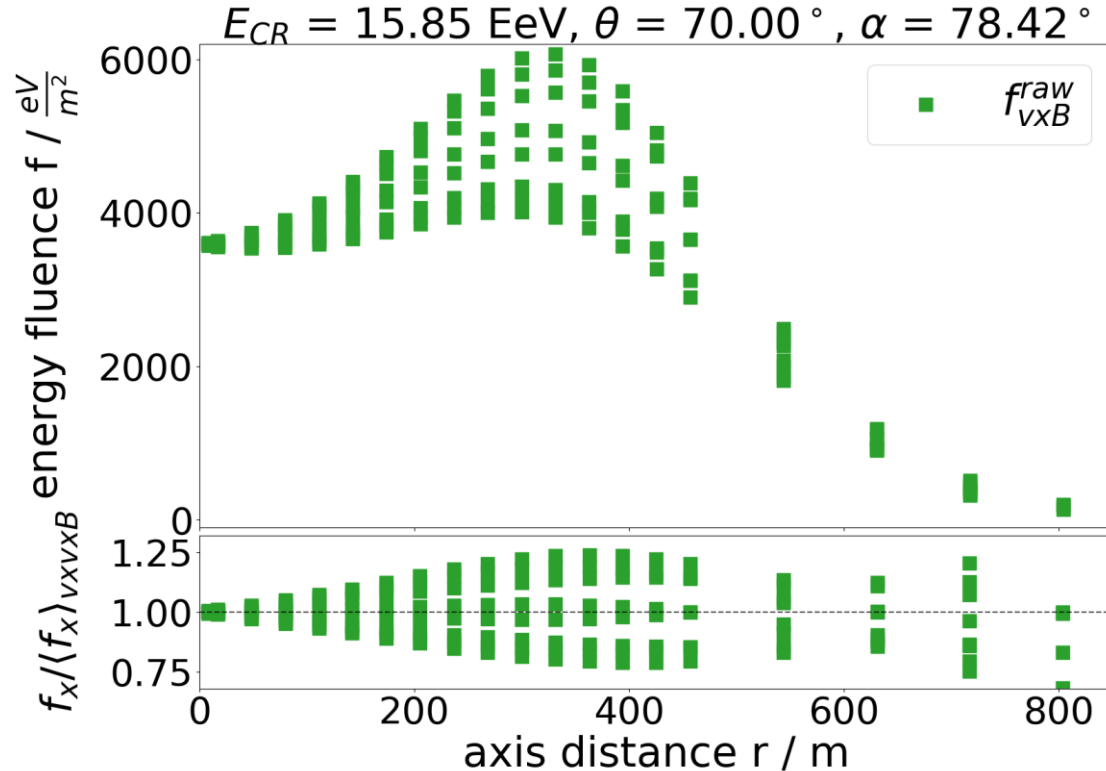
atmospheric density correction

- with this, we can calculate geomagnetic energy fluence at any location by subtraction of charge-excess fluence from $\mathbf{v} \times \mathbf{B}$ measurement

$$f_{\text{geo}}^{\text{par}} = \frac{f_{\mathbf{v} \times \mathbf{B}}}{\left(1 + \frac{\cos(\phi)}{|\sin(\alpha)|} \cdot \sqrt{a(r, d_{\max}, \rho_{\max})}\right)^2}$$

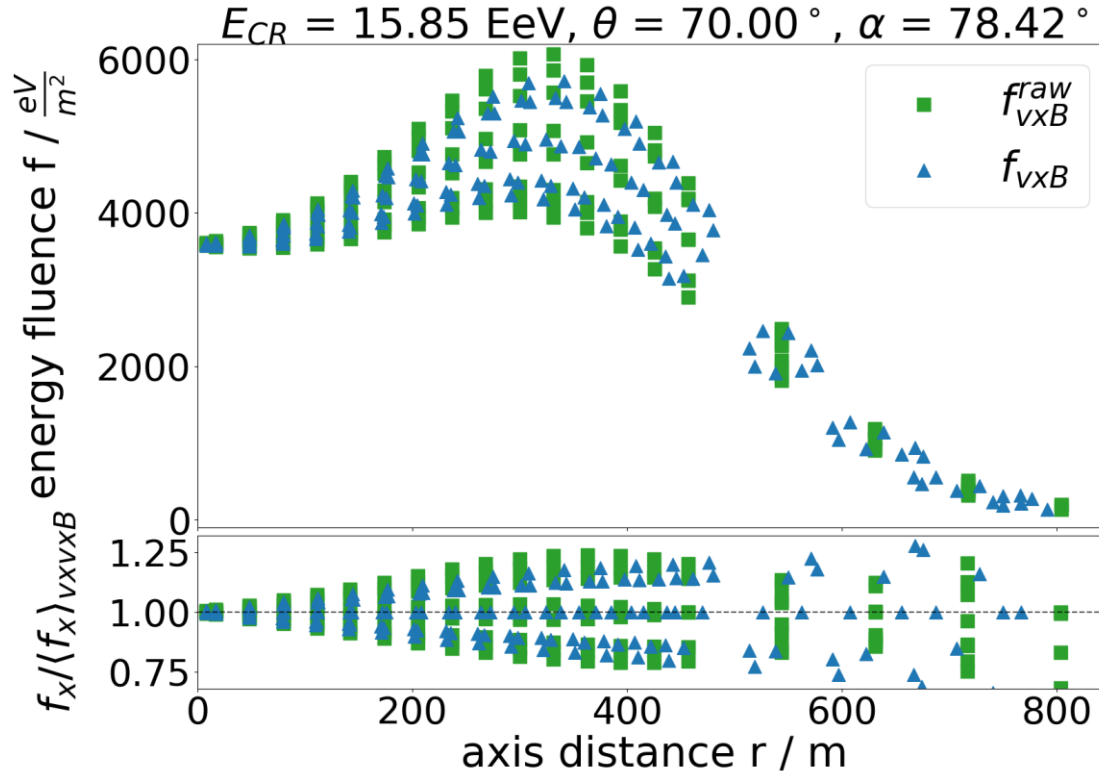
cf. Glaser et al. JCAP 09 (2016) 024 and
Astroparticle Physics 104 (2019) 64-77

Performance of charge-excess correction



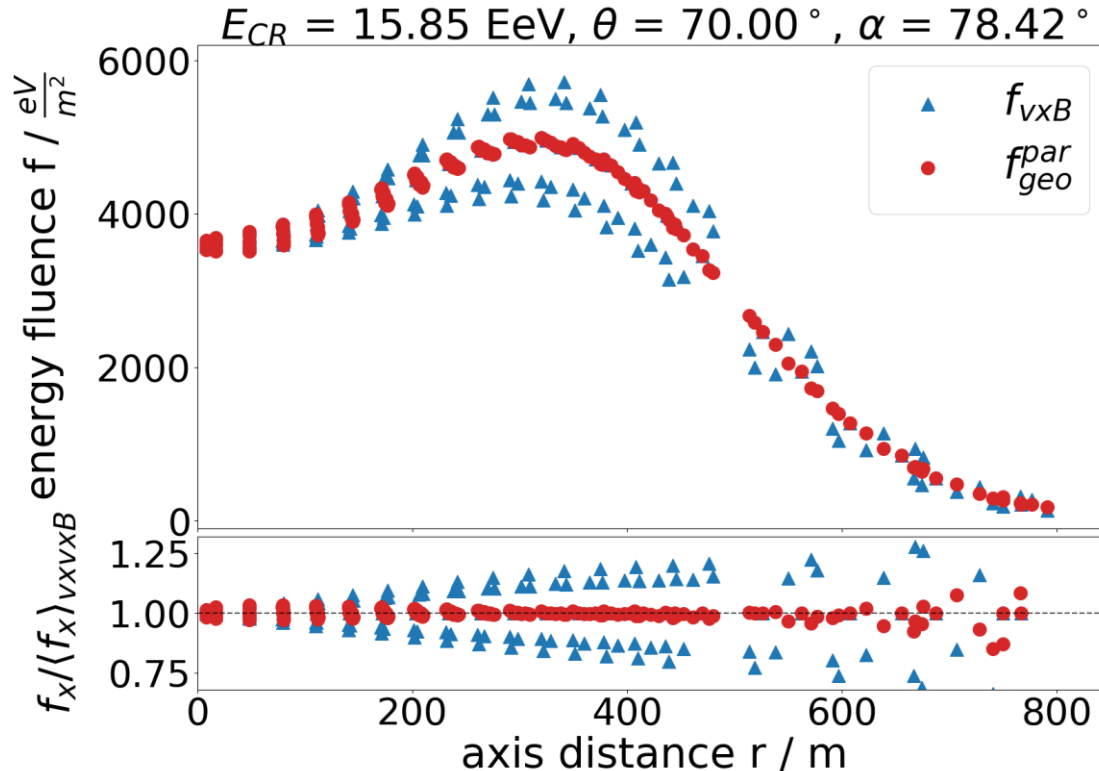
- application of early-late correction and charge-excess correction results in a mostly symmetric LDF
- some scatter remains, arising from deviations from circular symmetry of charge-excess fraction

Performance of charge-excess correction



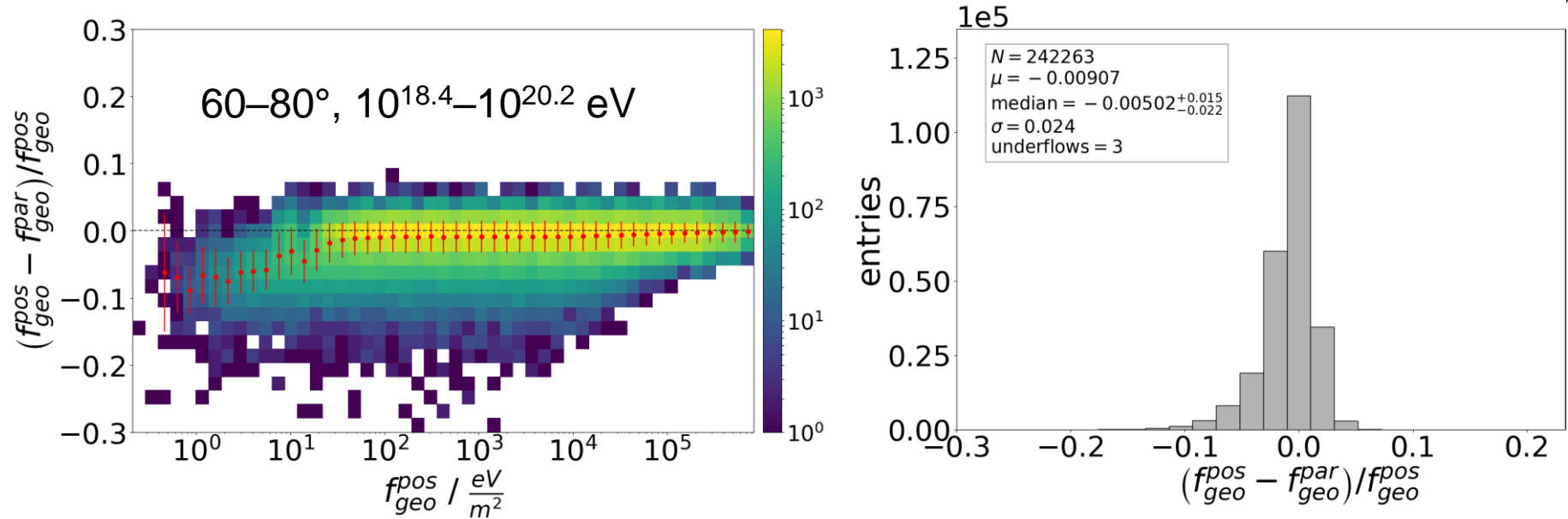
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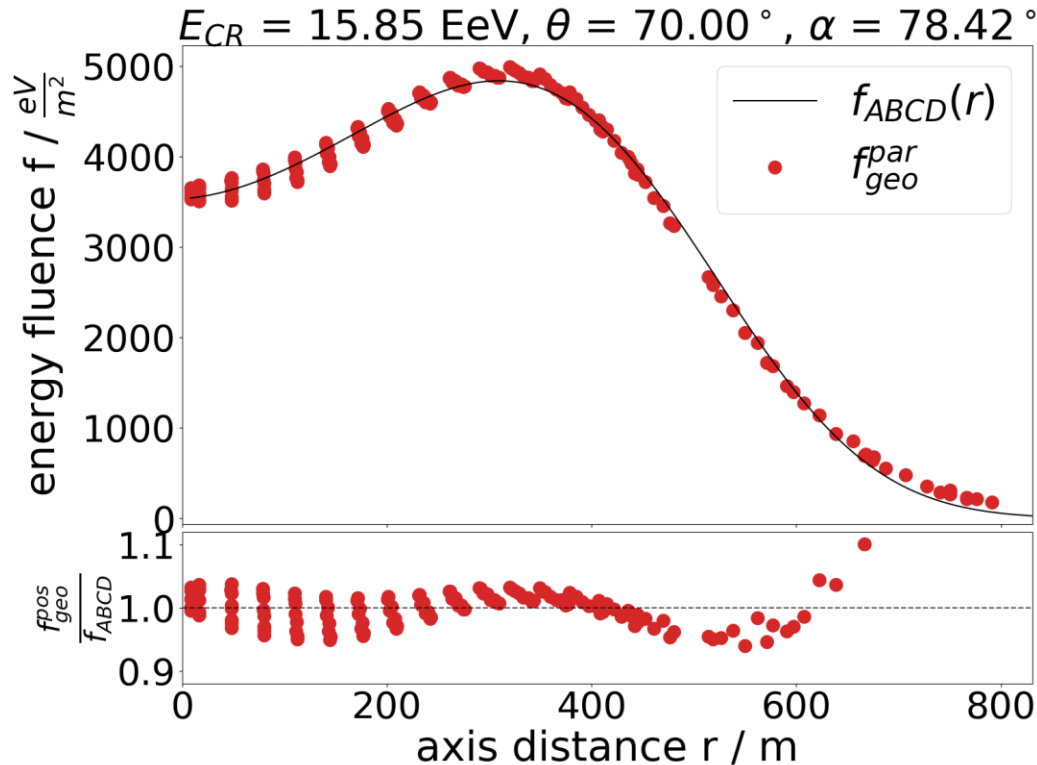
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Overall performance of symmetrization



- average bias for all showers is below 1%, spread below 2.5%
- deviations from true geomagnetic energy fluence only at small values (not relevant for the radiation energy integration)

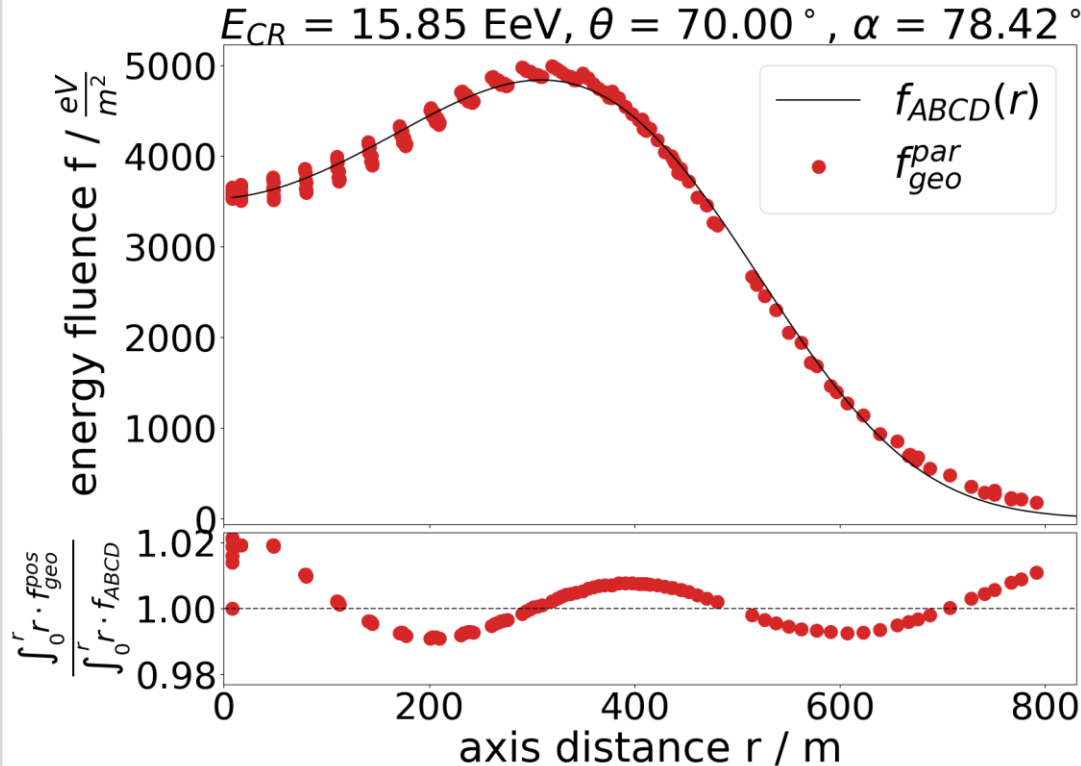
Fitting a rotationally symmetric LDF



- canonical exponential of a cubic polynomial works well

$$f_{ABCD}(r) = A \cdot \exp \left[-B \cdot r - C \cdot r^2 - D \cdot r^3 \right]$$
- some deviations at large lateral distances, but minor influence on radiation energy integration

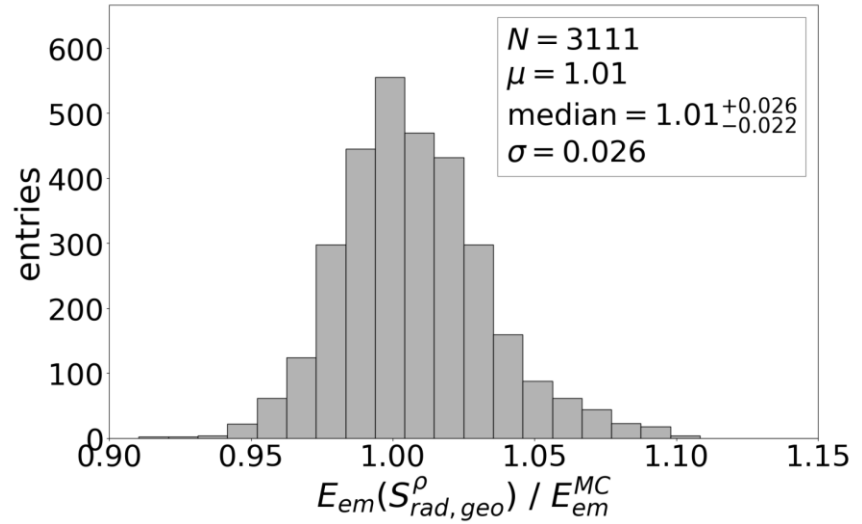
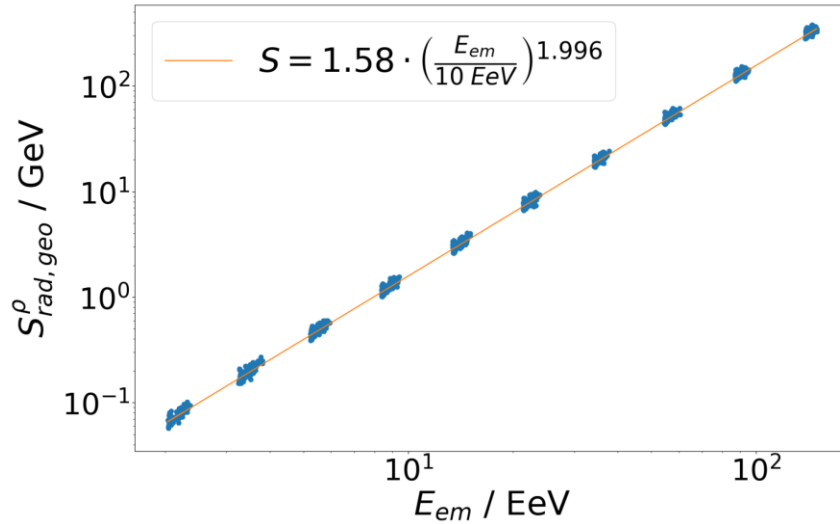
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Radiation energy integration via fitted LDF

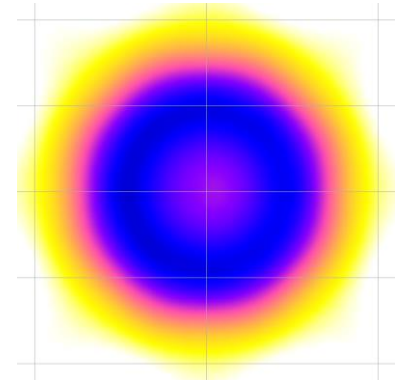
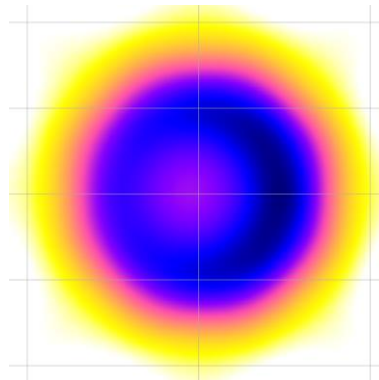
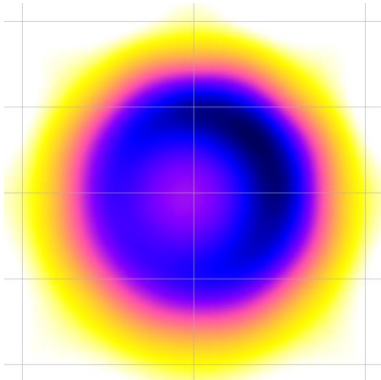


- density-corrected geomagnetic radiation energy correlates well with energy in the electromagnetic cascade, spread smaller than 3%

$$S_{rad,geo}^\rho = \frac{E_{rad}^{geo}}{\sin^2(\alpha)} \cdot \frac{1}{1 - p_0 + p_0 \cdot \exp[p_1 \cdot (\rho - \langle \rho \rangle)]}$$

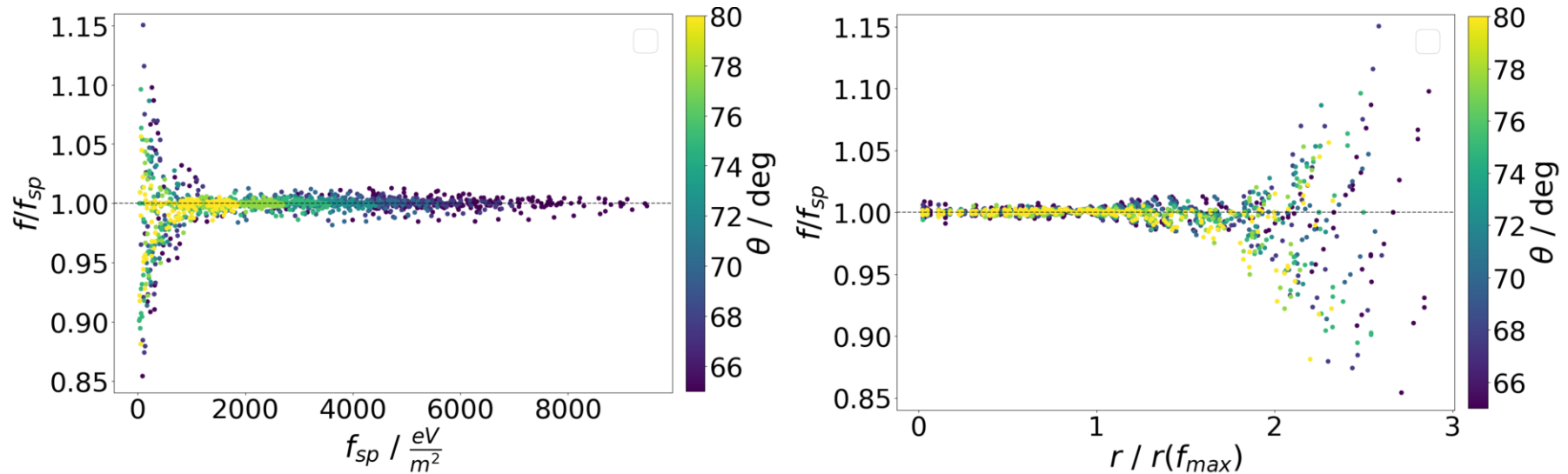
Conclusion

- radio signal distribution of inclined air showers is highly asymmetric
- have developed analytic model to symmetrize the distribution
- symmetrized distribution can be fit with simple 1d LDF
- integration over 1d LDF yields *geomagnetic radiation energy*
- 3% intrinsic energy resolution in 30-80 MHz band and for $\theta = 60-80^\circ$
- will develop event reconstruction on this basis



Backup

Performance of early-late correction



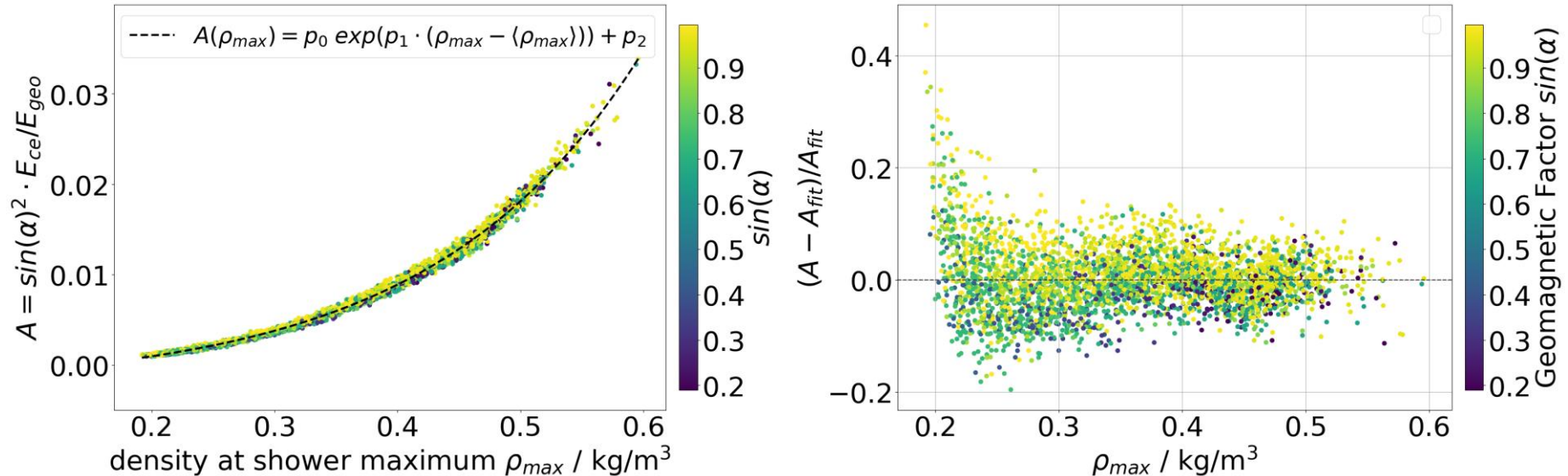
- most significant deviations are at large lateral distances and small energy fluences

Determining charge-excess fraction directly

$$f_{\text{geo}}^{\text{pos}} = \left(\sqrt{f_{\mathbf{v} \times \mathbf{B}}} - \frac{\cos(\phi)}{|\sin(\phi)|} \cdot \sqrt{f_{\mathbf{v} \times \mathbf{v} \times \mathbf{B}}} \right)^2$$
$$f_{\text{ce}}^{\text{pos}} = \frac{1}{\sin^2(\phi)} \cdot f_{\mathbf{v} \times \mathbf{v} \times \mathbf{B}}.$$

- for a given observation position, the charge-excess fraction can be determined directly via the known polarisation characteristics of the geomagnetic and charge-excess contributions, cf. Glaser et al., Astroparticle Physics 104 (2019) 64-77

Total CE fraction and density at Xmax



- *total* charge-excess fraction correlates with density at Xmax, see Glaser, Erdmann, Hörandel, Huege, Schulz, JCAP 09 (2016) 024