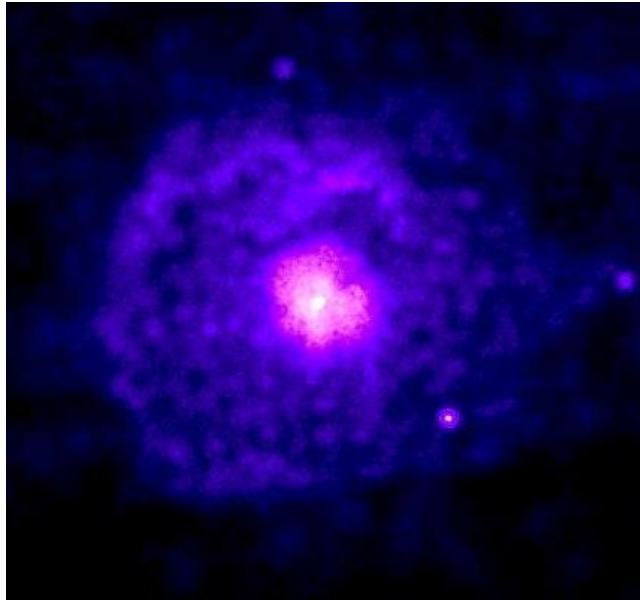


Modeling of Broadband Spectra and Radial Profiles of Emission of Pulsar Wind Nebulae



Wataru Ishizaki¹

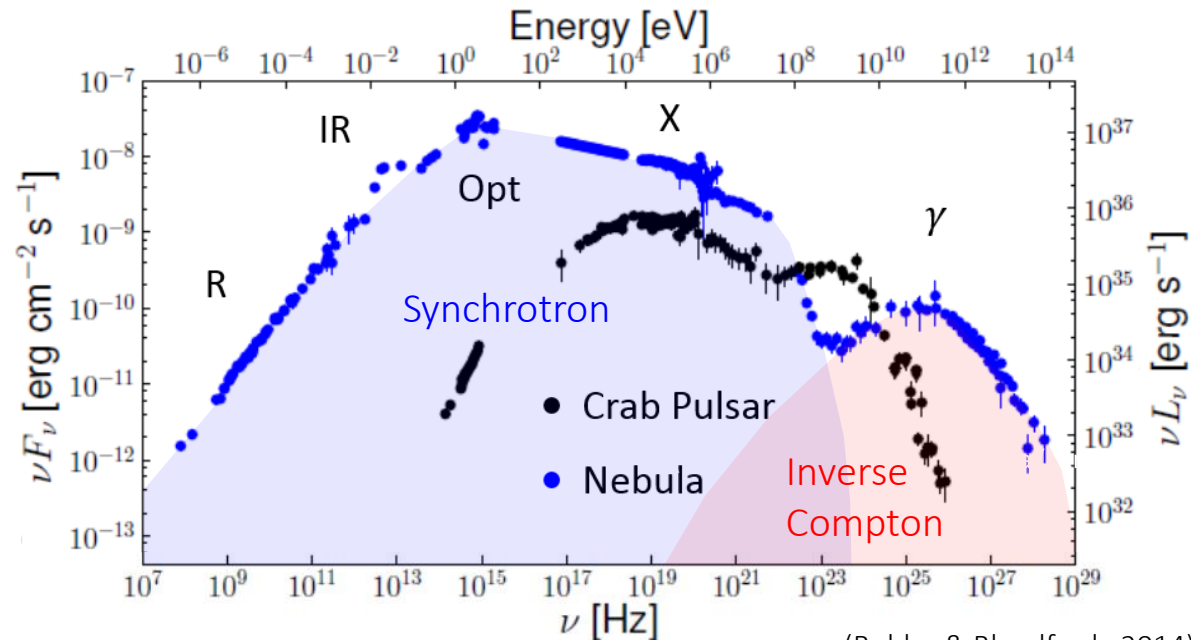
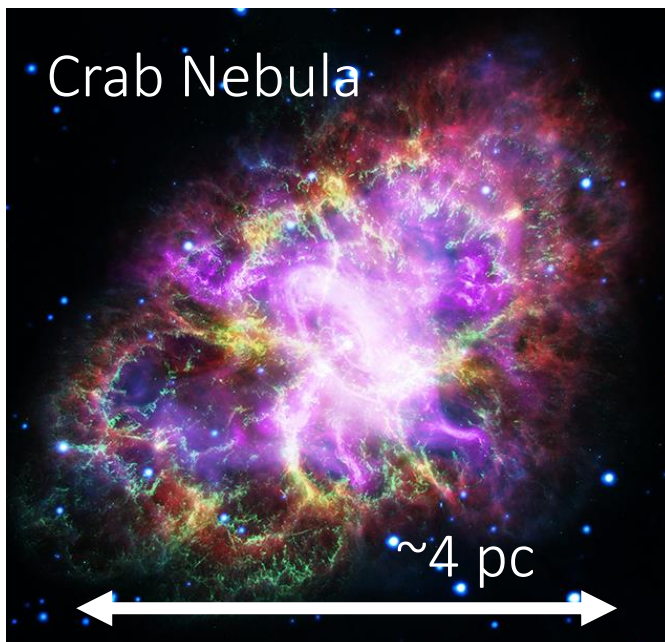
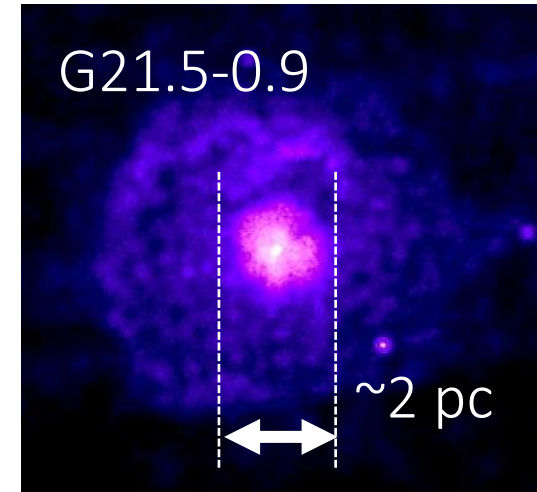
Katsuaki Asano², Kyohei Kawaguchi²

1. Yukawa Institute for Theoretical Physics (YITP)

2. Institute for Cosmic-Ray Research (ICRR)

Introduction –Pulsar Wind Nebulae-

- Pulsar Wind Nebulae (PWNe)
 - Extended source around a rotation powered pulsar
 - **Broadband non-thermal spectrum from radio to TeV- γ**
- Non-thermal emission
 - Radio – X : Synchrotron
 - γ -rays : Inverse Compton (external or SSC)
 - **X-ray photons are emitted by e^\pm with highest energy**

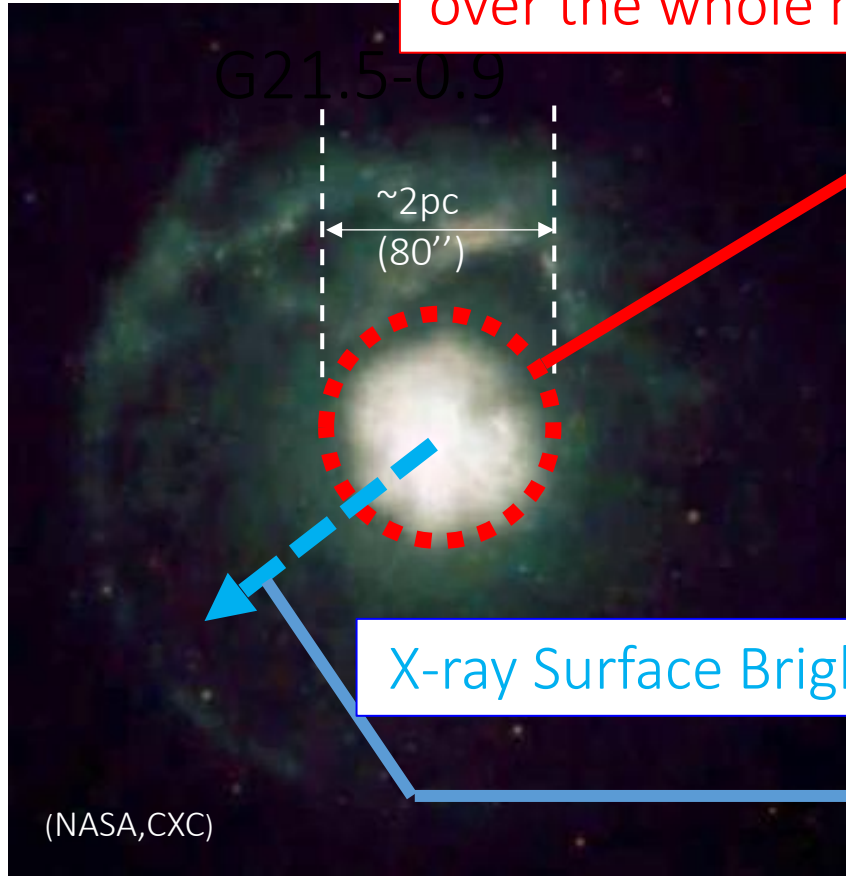


(Buhler & Blandford , 2014)

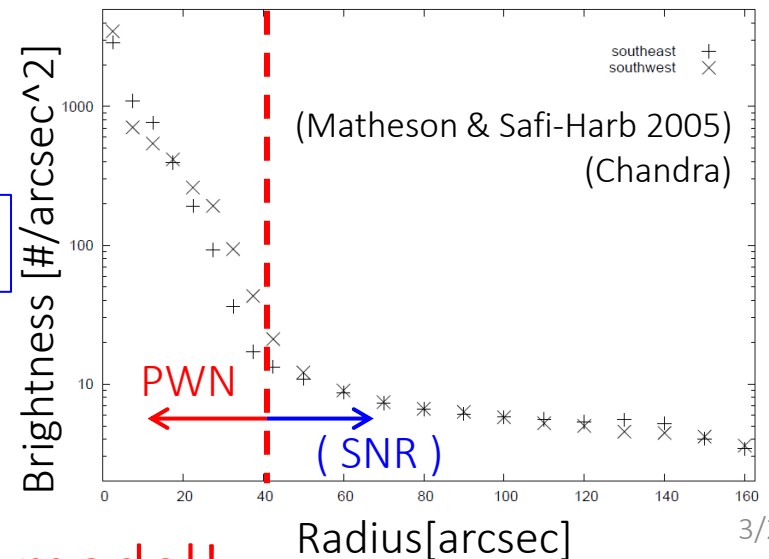
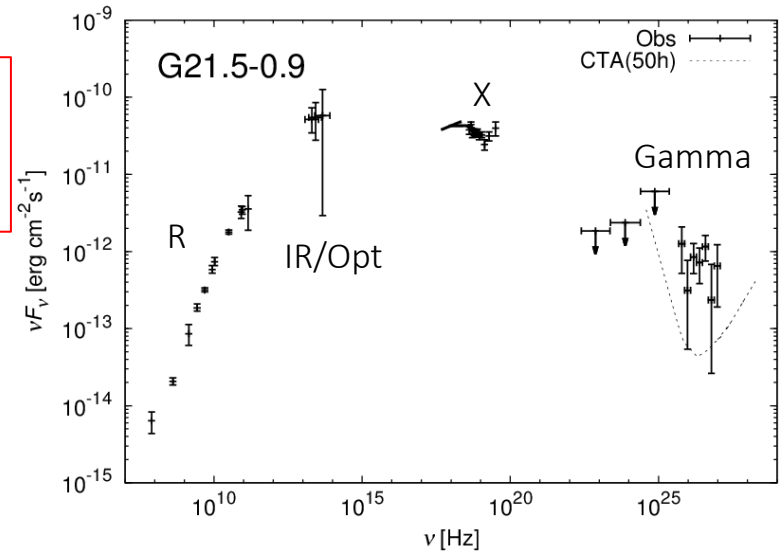
Observed Quantities

- eg. G21.5-0.9

Spectrum integrated over the whole nebula



X-ray Surface Brightness

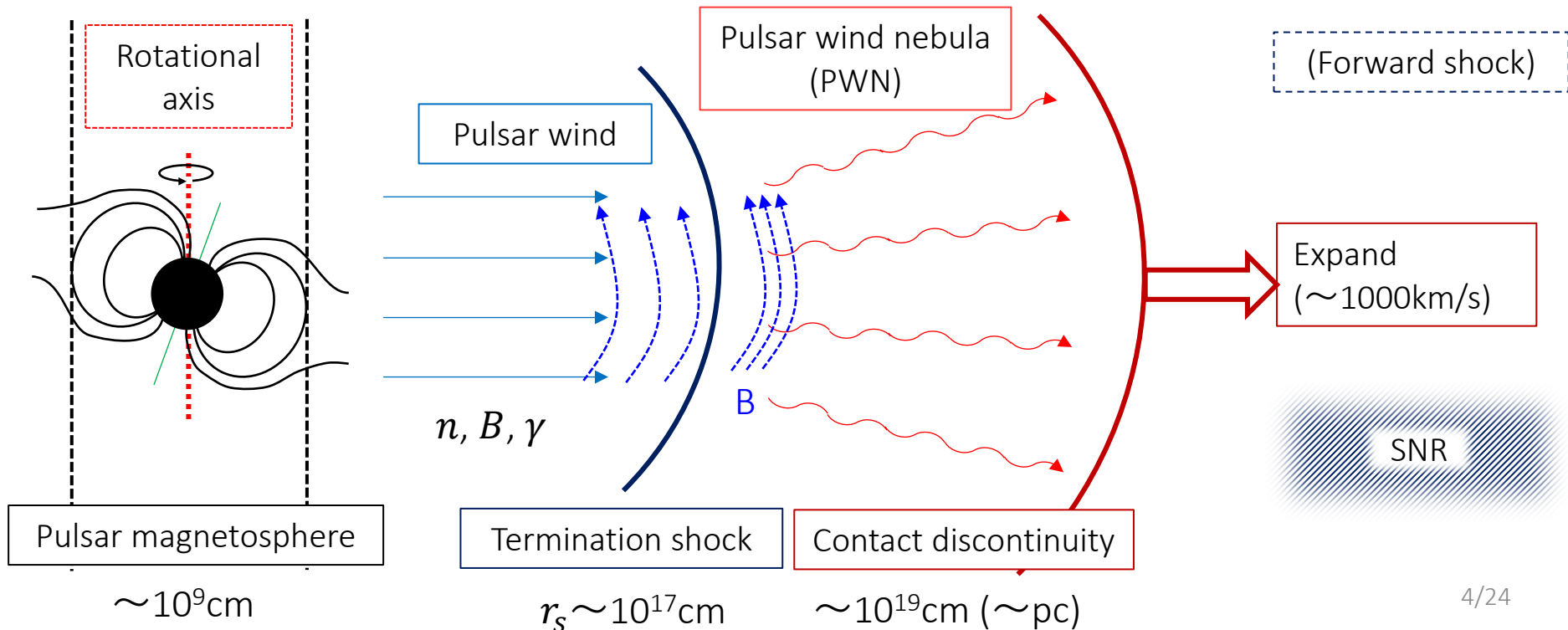
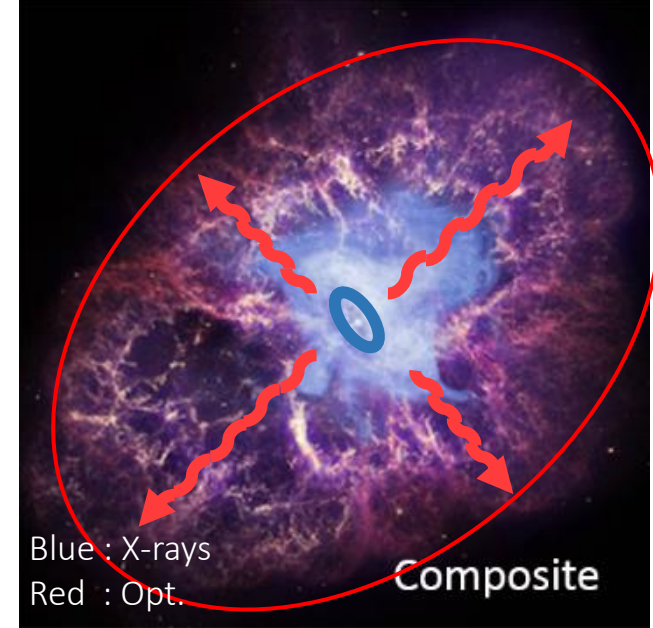


Most simplified spatial model \rightarrow 1D model!

“Standard model” of PWNe

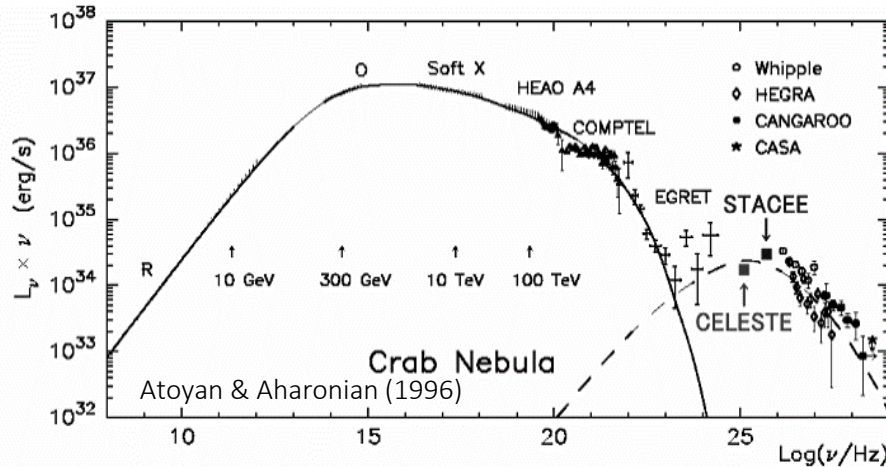
- 1D-steady model ; Rees & Gunn (1974), Kennel & Coroniti (1984)
 - Assuming a radial flow and a toroidal field.
 - Non-thermal e^\pm produced at termination shock r_s
 - Propagating in PWN with radiative cooling
 - Non-thermal e^\pm only advect with flow

Well explains observed property of the Crab Nebula

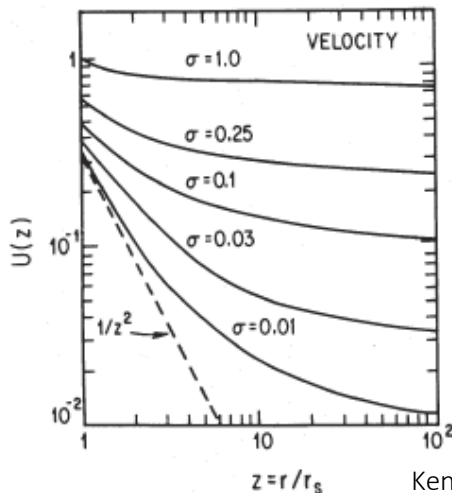


What KC model explains

- SED (Spectrum of the whole nebula)



- Deceleration of the flow



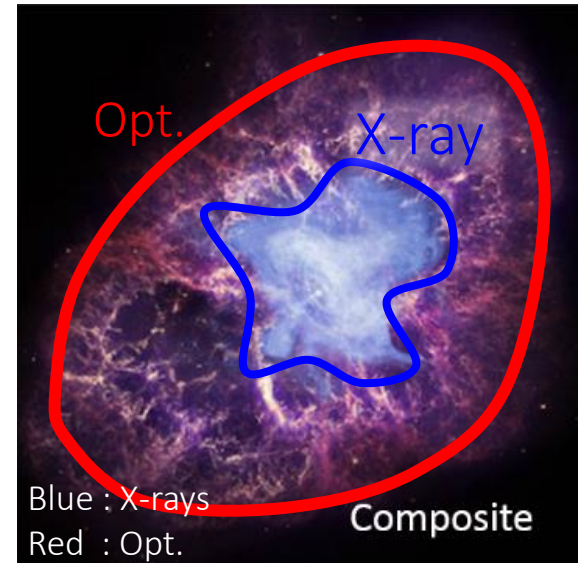
@shock : $\sim c/3$

@edge : ~ 1000 km/s

Q. How decelerates ?

A. Low sigma flow

- Energy dependent morphology



KC model can explain these properties

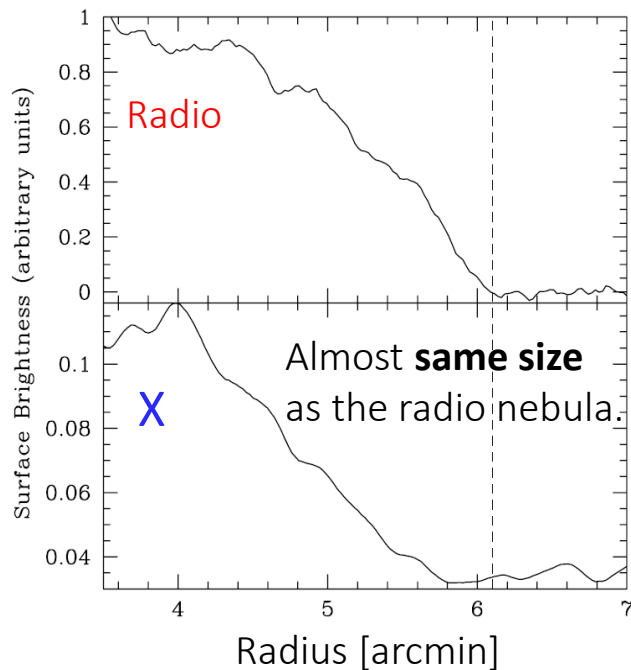
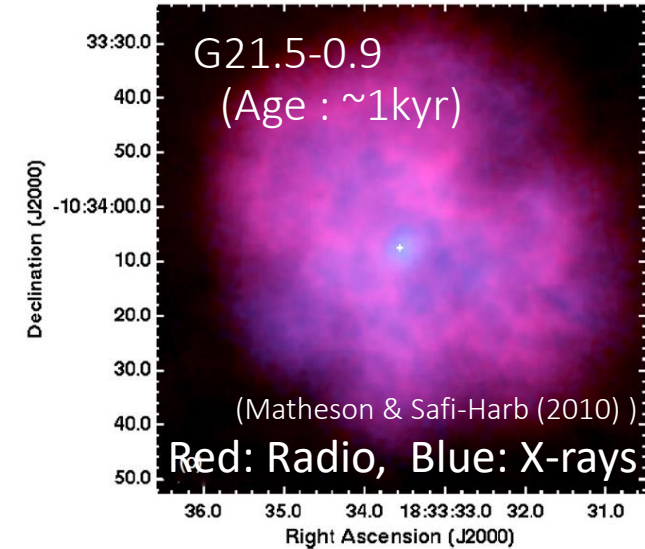
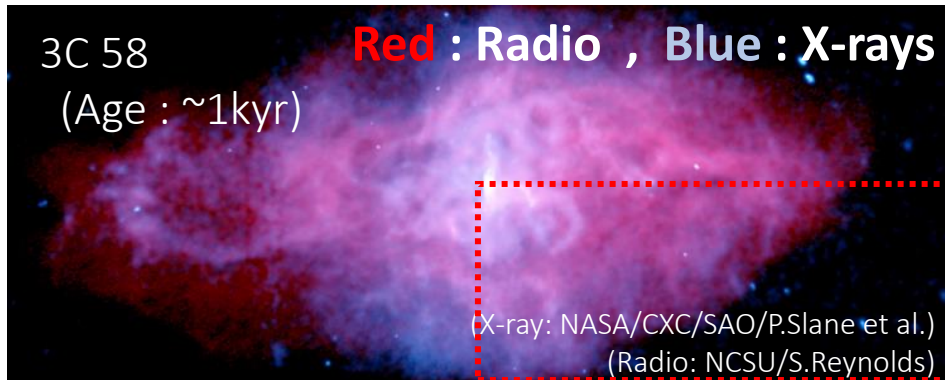
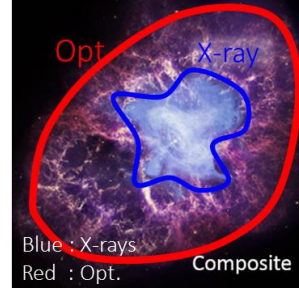
→ KC model was accepted as a standard model

However, such a test has performed for the Crab Nebula **ONLY**.

cf. the Crab Nebula

3C 58, G21.5-0.9

PWNe which show large extent of X-ray emission (**unlike** the Crab Nebula).



Q : Can these observation explain by KC model?

A : Lack of information.

It is necessary to calculate the SED and constraint the parameters.

Can KC model reproduce
SED & X-ray profile **simultaneously**?

Test of KC model

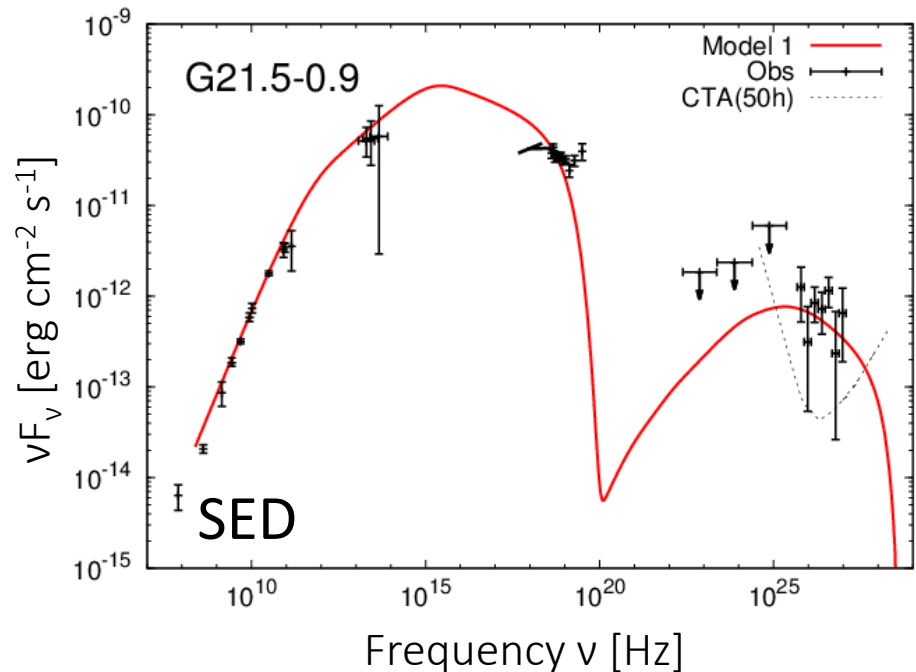
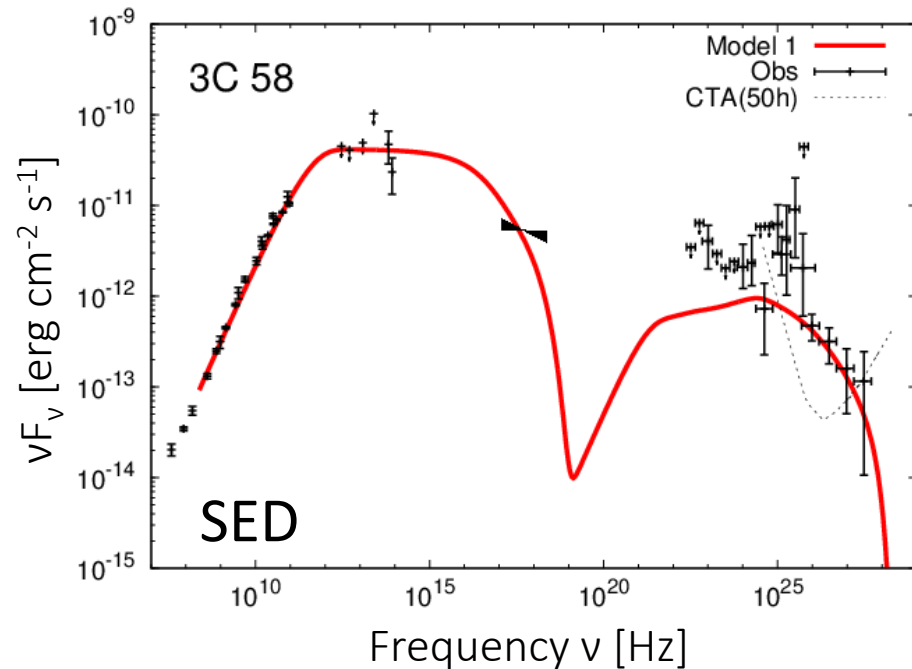
See Ishizaki+17 (ApJ, arXiv: 1703.05763) for detail

- SED
- X-ray surface brightness
- X-ray photon index

Test of KC model

See Ishizaki+17 (ApJ, arXiv: 1703.05763) for detail

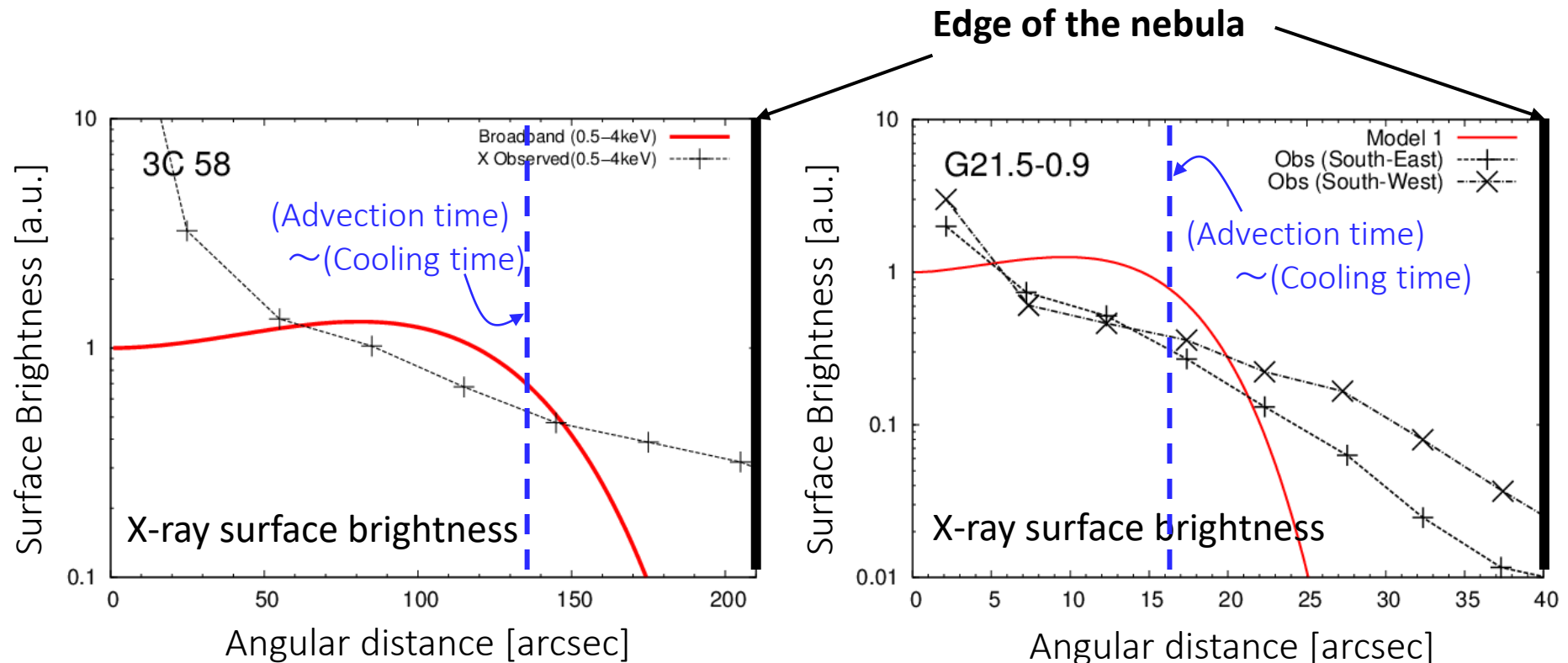
- **SED** : almost reproduced w/ KC model
 - Obtained the parameters almost uniquely
- X-ray surface brightness
- X-ray photon index



Test of KC model

See Ishizaki+17 (ApJ, arXiv: 1703.05763) for detail

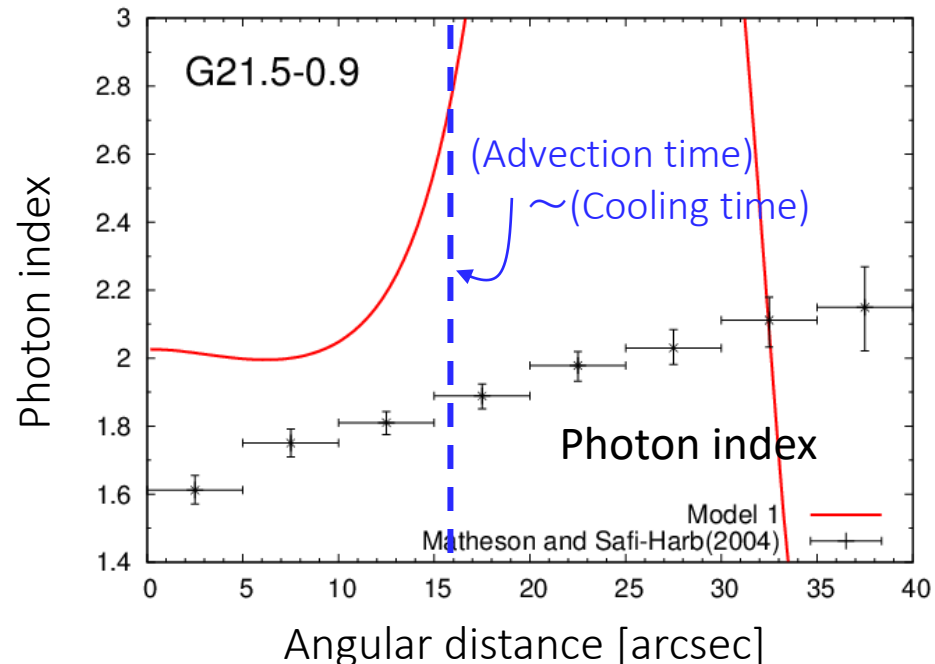
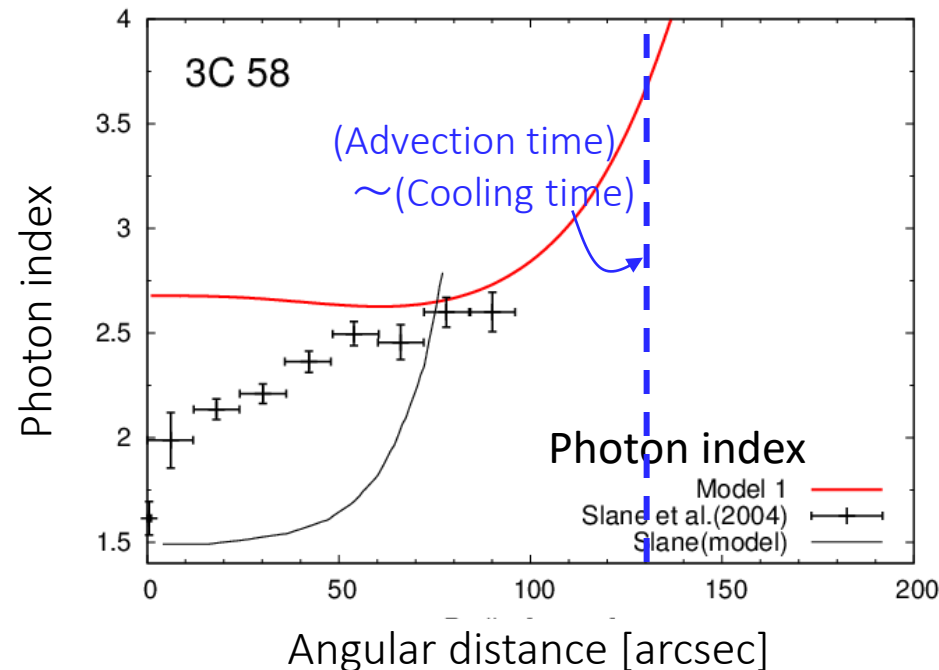
- SED : almost reproduced w/ KC model
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- X-ray surface brightness : NOT reach the edge
 - High energy e^\pm exhaust their energy by emission.
- X-ray photon index



Test of KC model

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- SED : almost reproduced w/ KC model
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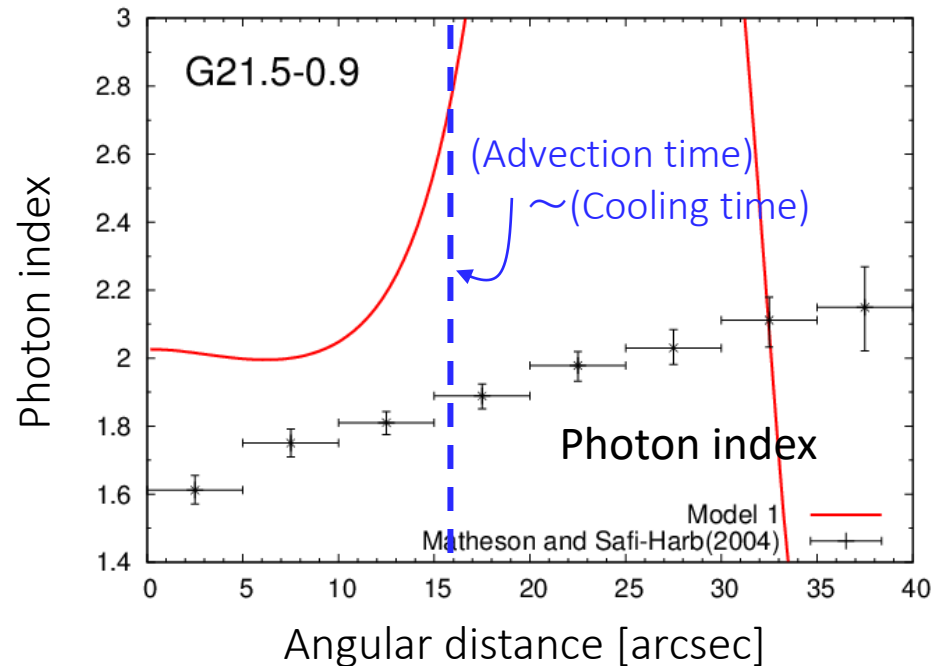
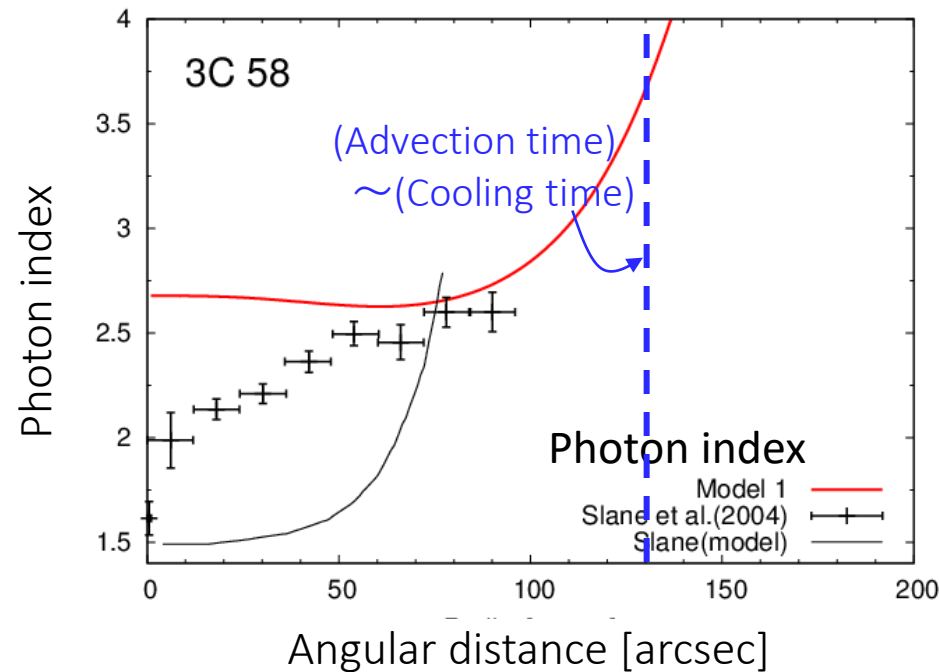
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OK

NG



Test of KC model

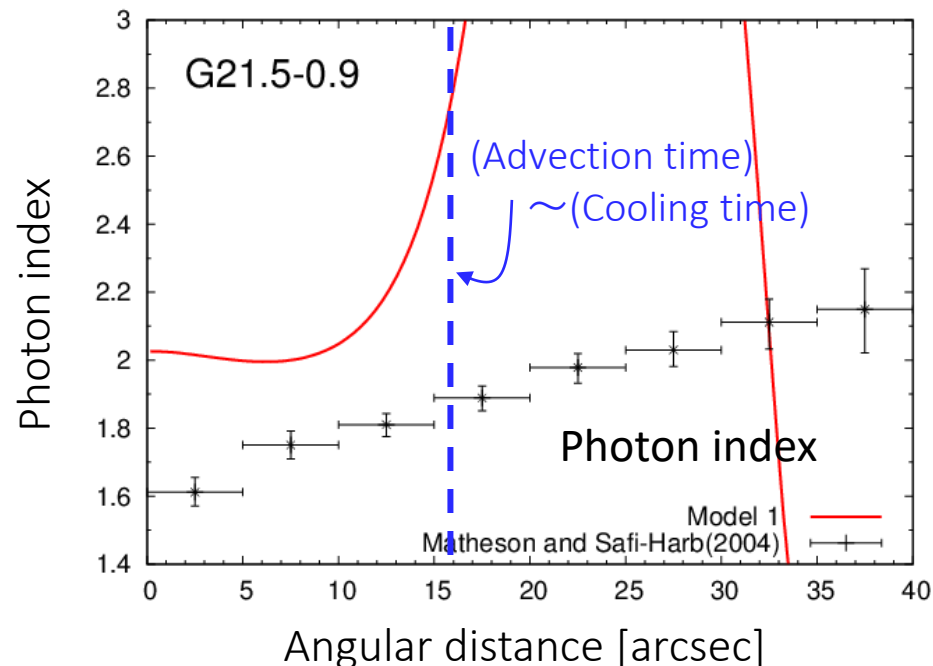
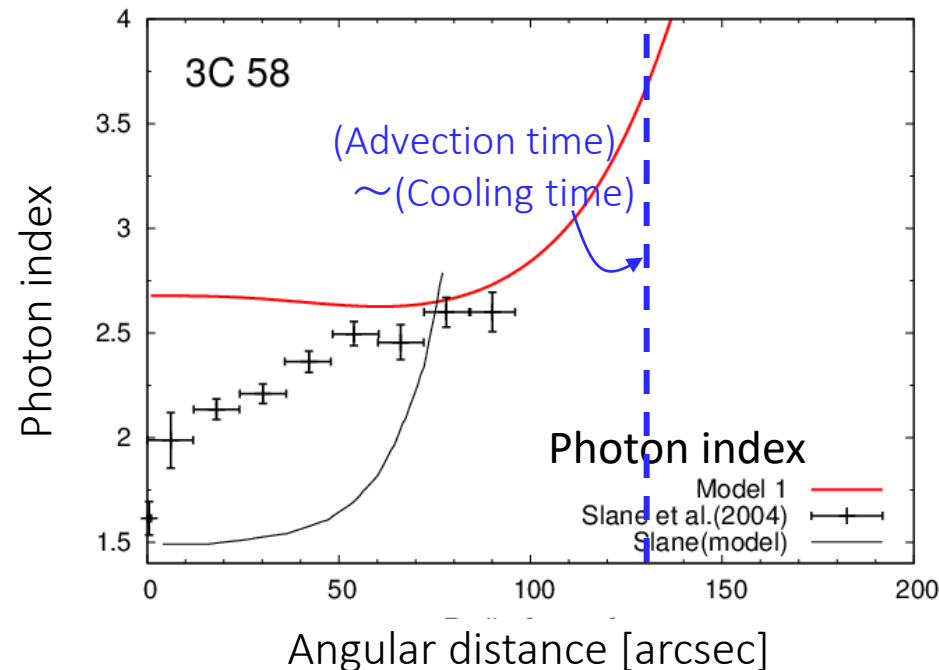
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OK

NG

KC model **CANNOT** reproduce SED and X-ray profile simultaneously!



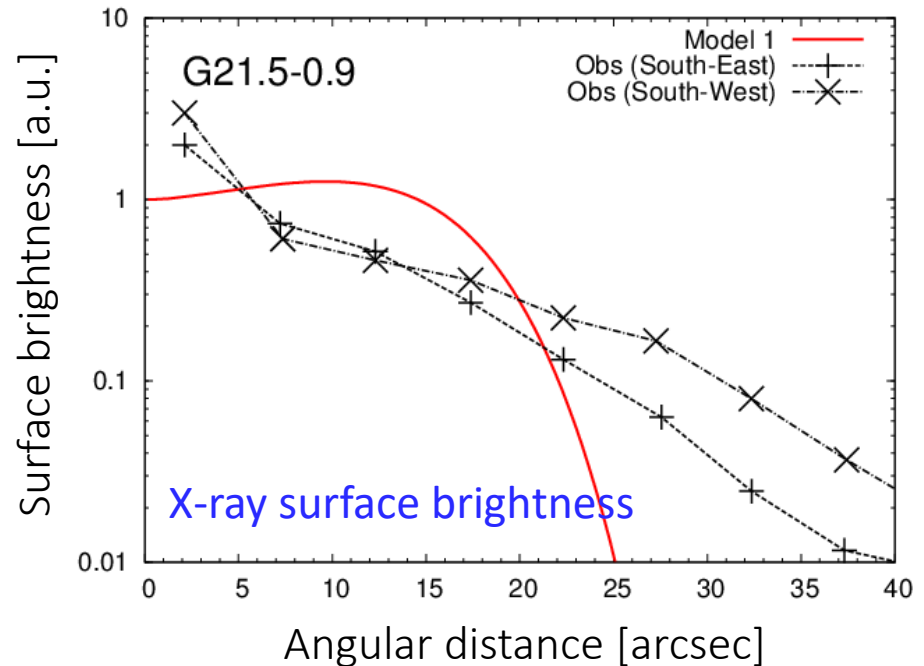
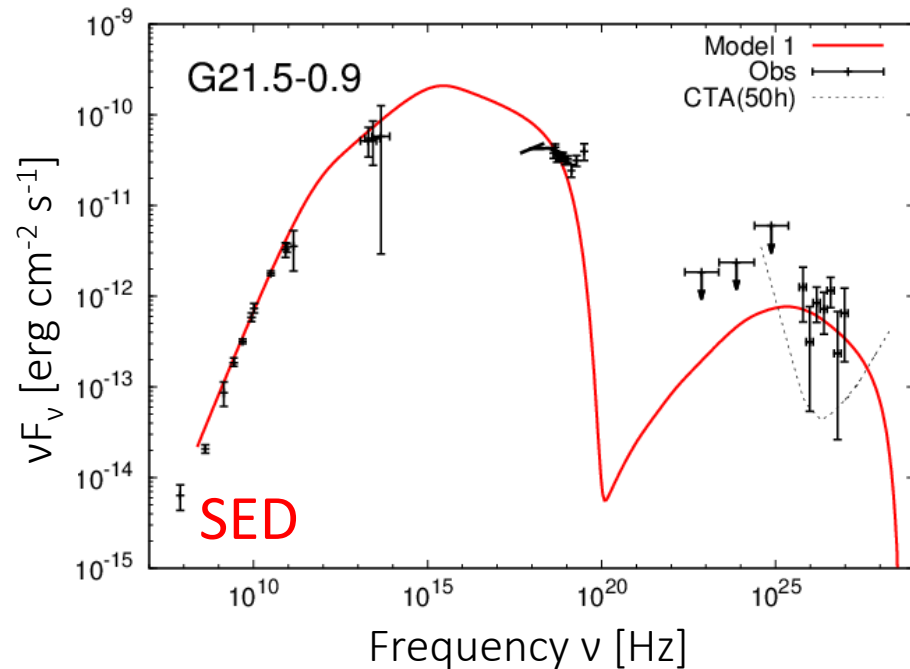
Why cannot?

Why cannot?

“Magnetic Field to reproduce the SED” > “Magnetic field to reproduce the X-ray extent”

How do we do?

B-field to reproduce SED : determined from the flux ratio of synchrotron and ICS.



Why cannot?

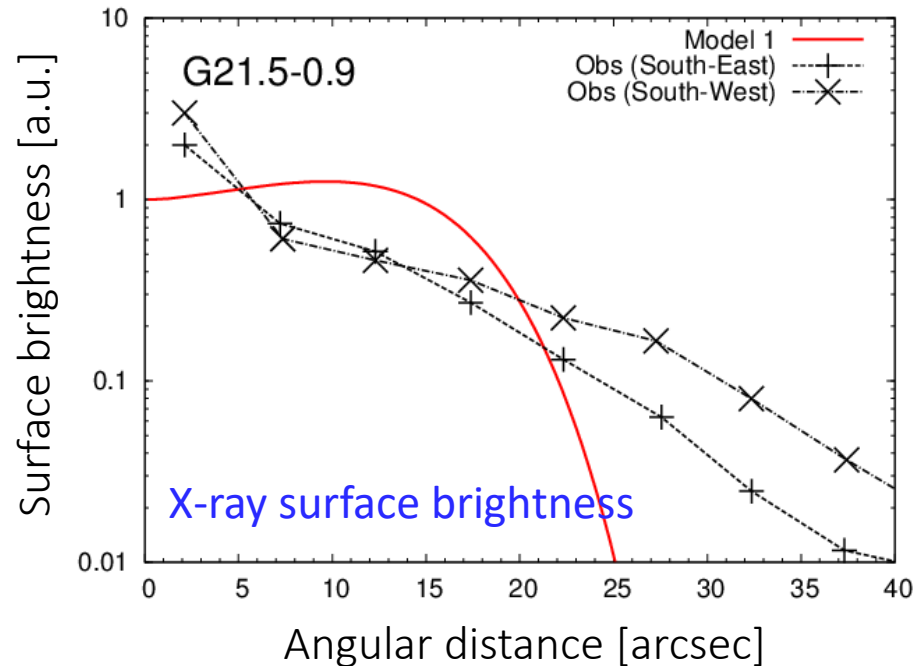
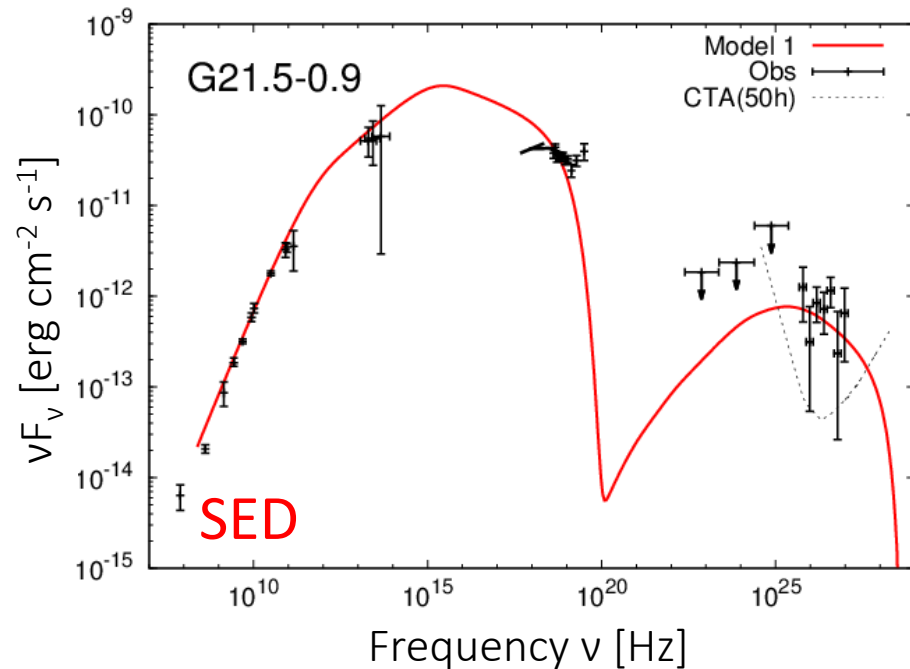
Determined by the balance of cooling and advection time

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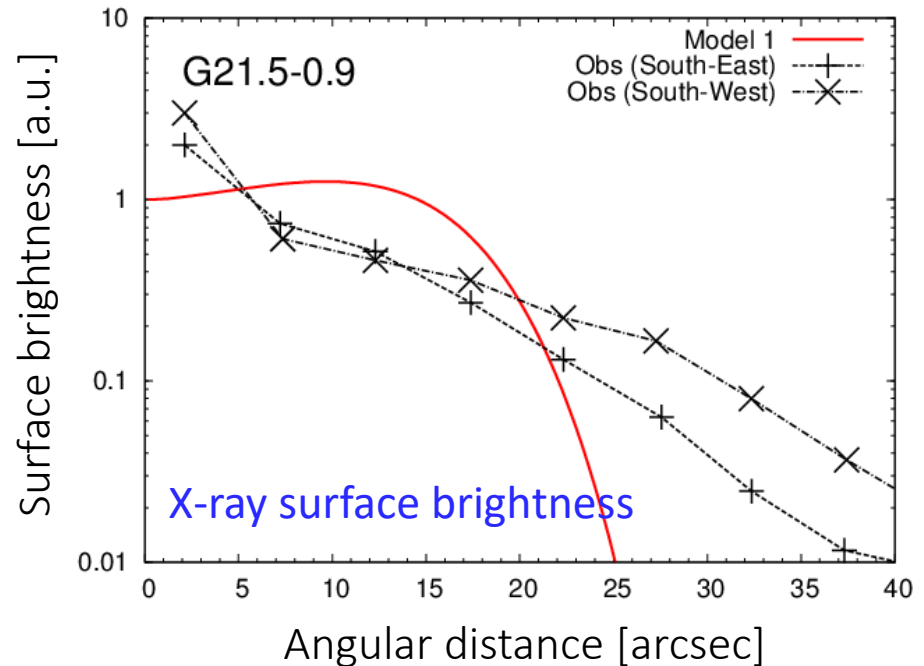
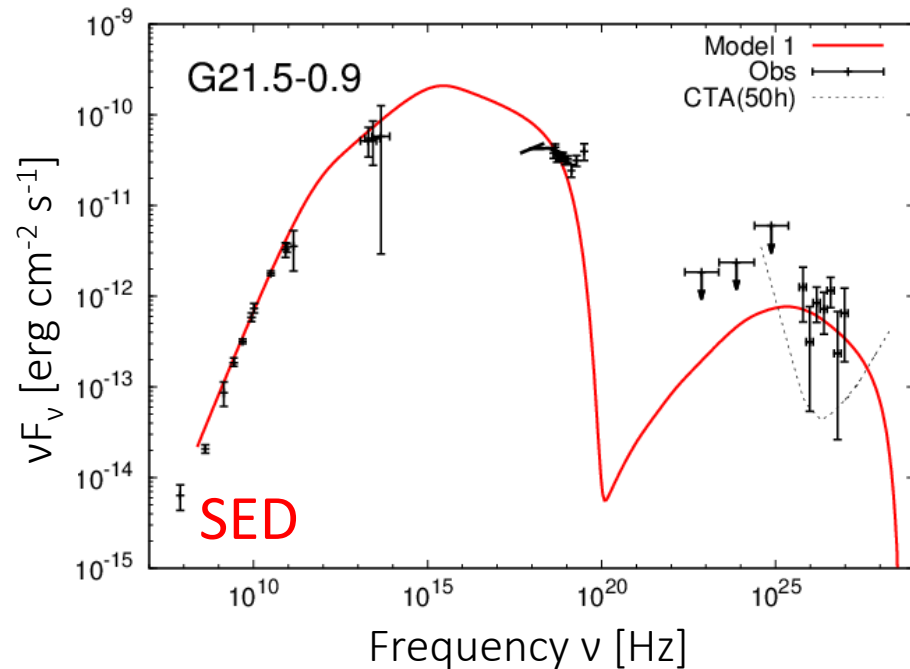
Fixed

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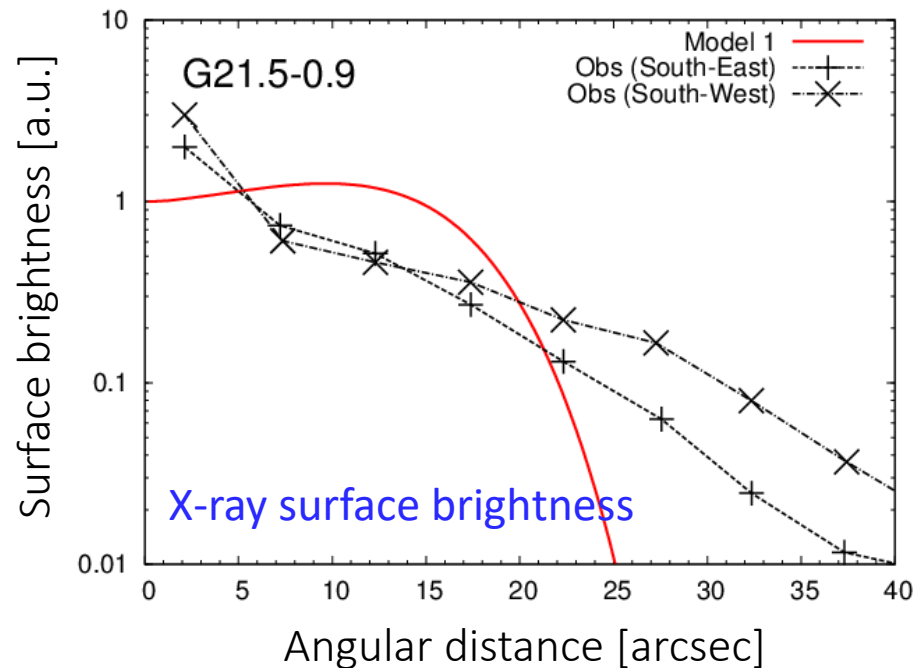
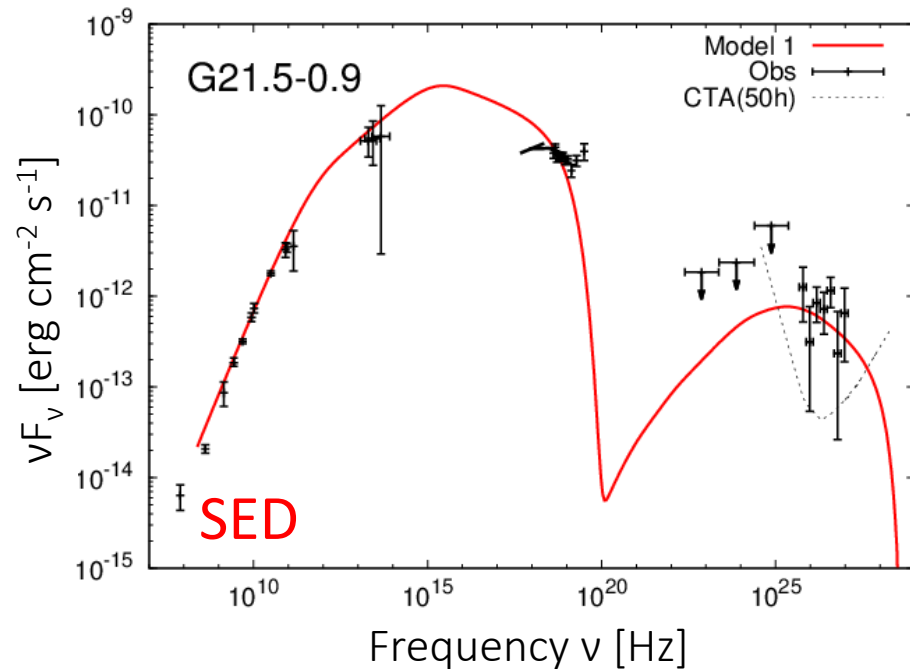
Why cannot?

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How do we do?

B-field to reproduce SED : determined from the flux ratio of synchrotron and ICS.

⇒ It is necessary to propagate outward more efficiently. (rather than to suppress cooling)



Efficient transport?

- To solve the problem of X-ray extent...

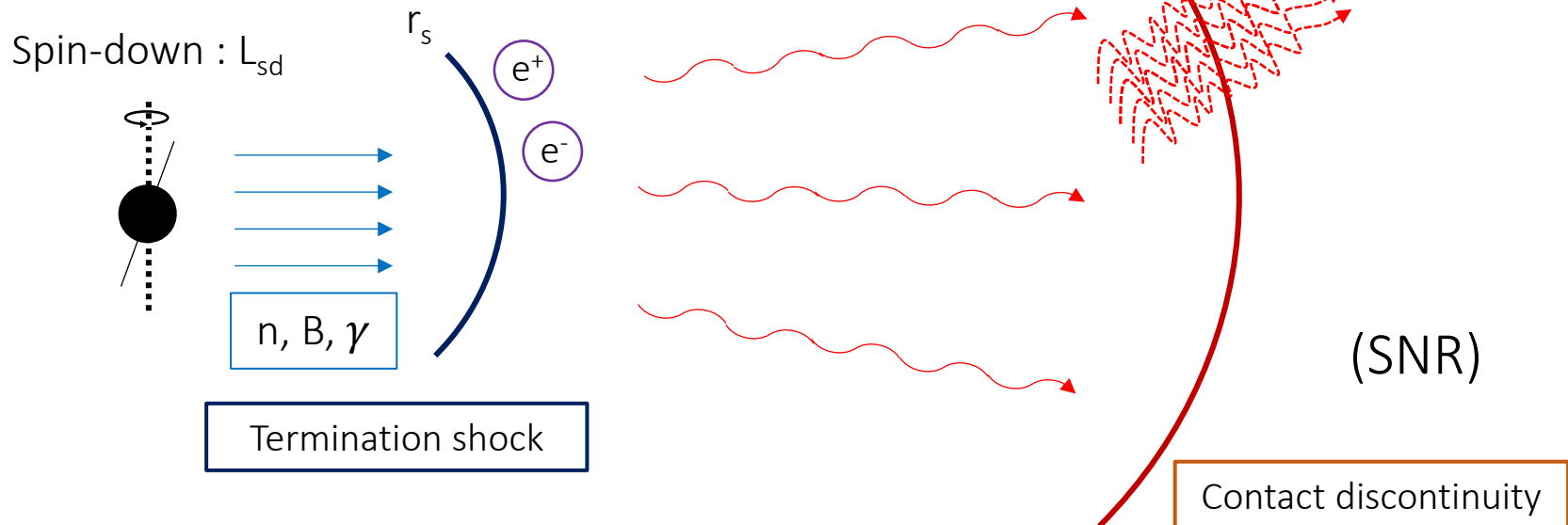
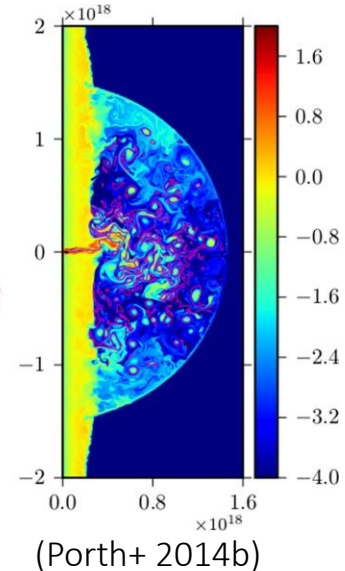
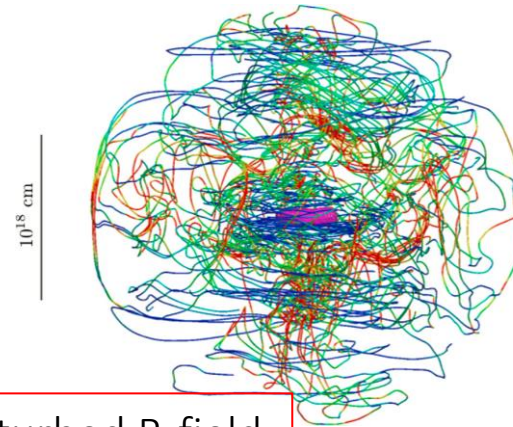
A) Suppress the radiative cooling

B) Transport efficiently

⇒ Spatial diffusion by interacting with disturbed B-field

(Tang & Chevalier 2012, Porth+ 2016)

2-D, 3-D simulation



Efficient transport?

- To solve the problem of X-ray extent...

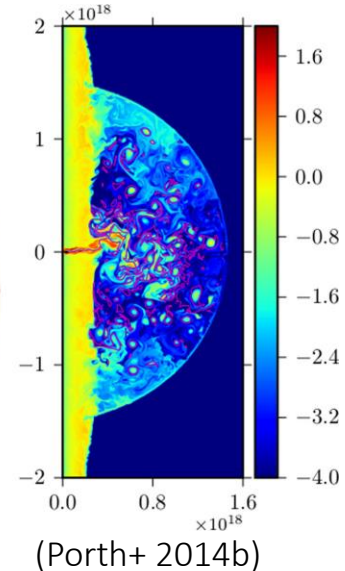
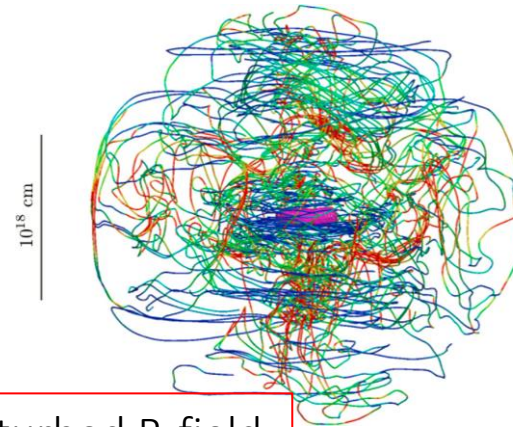
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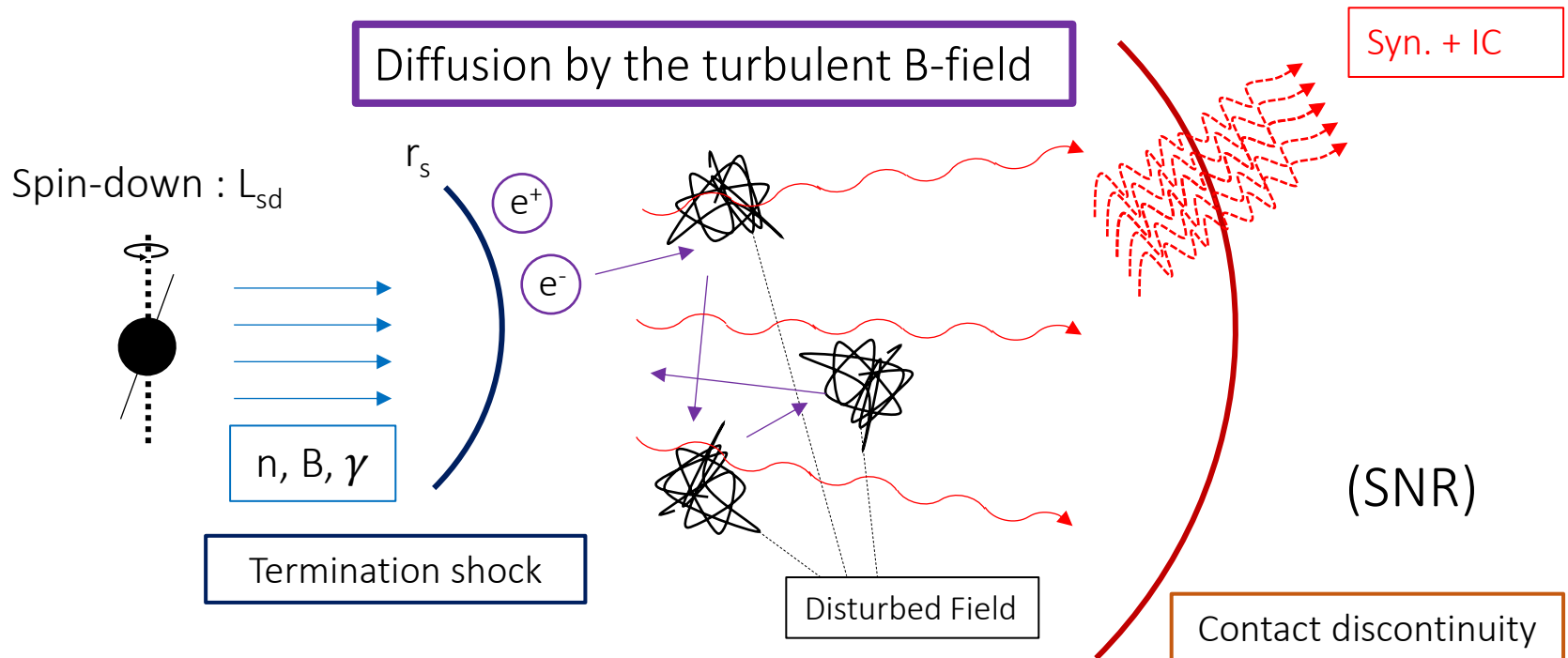
(Tang & Chevalier 2012, Porth+ 2016)

2-D, 3-D simulation



Let us consider the situation

"While advecting with the fluid, deviating from the fluid by diffusion little by little."



Result -G21.5-0.9-

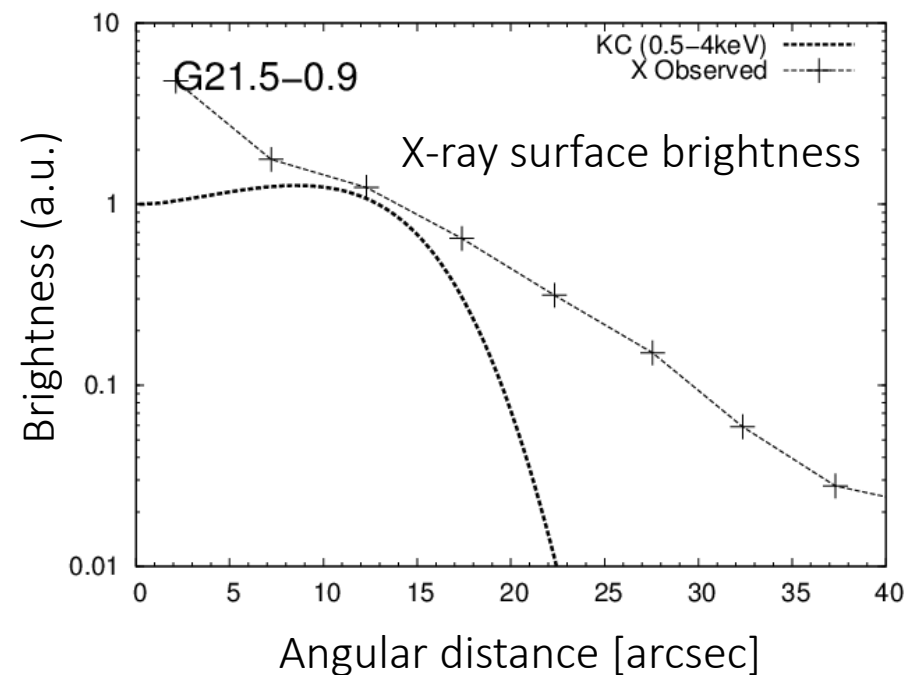
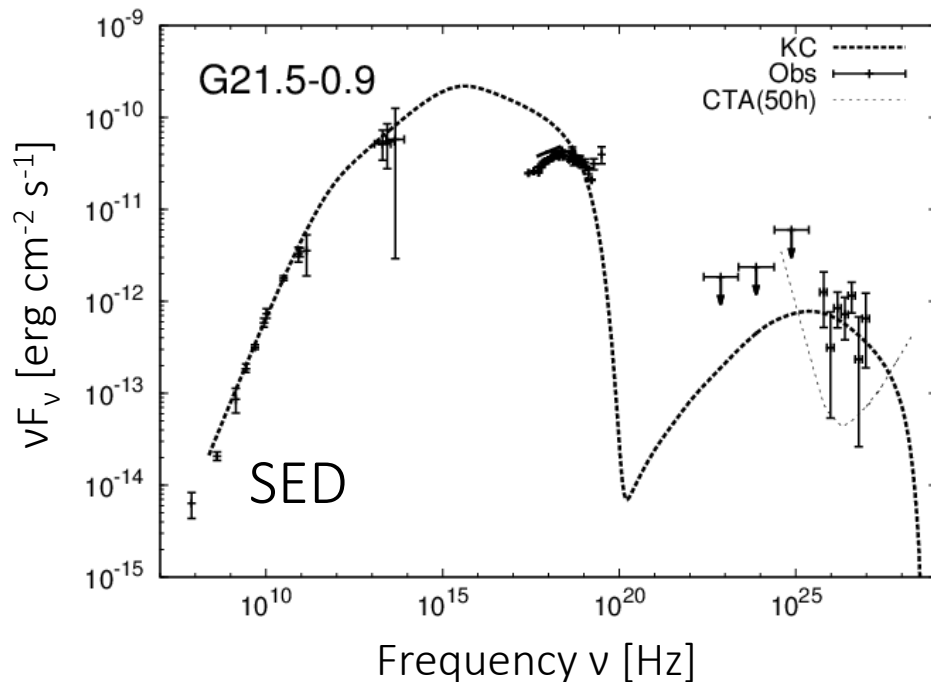
$$\tilde{\kappa} = \kappa_0 \left(\frac{E}{E_b} \right)^{1/3}$$

- Result for G21.5-0.9 (Omitted 3C 58)

diffusion coefficient of X-ray emitting particles : $\kappa \sim 10^{27} \text{ cm}^2 \text{ s}^{-1}$ Consistent with previous models

SED : The hard spectrum of X-rays is reproduced better (than KC).

See Ishizaki+18 (ApJ, arXiv: 1809.09054) for detail



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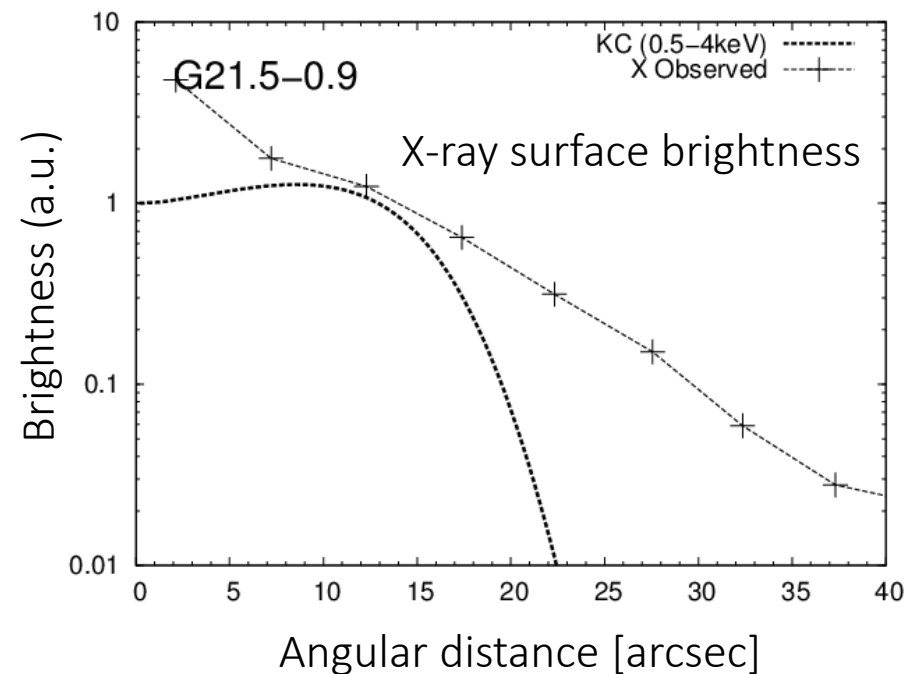
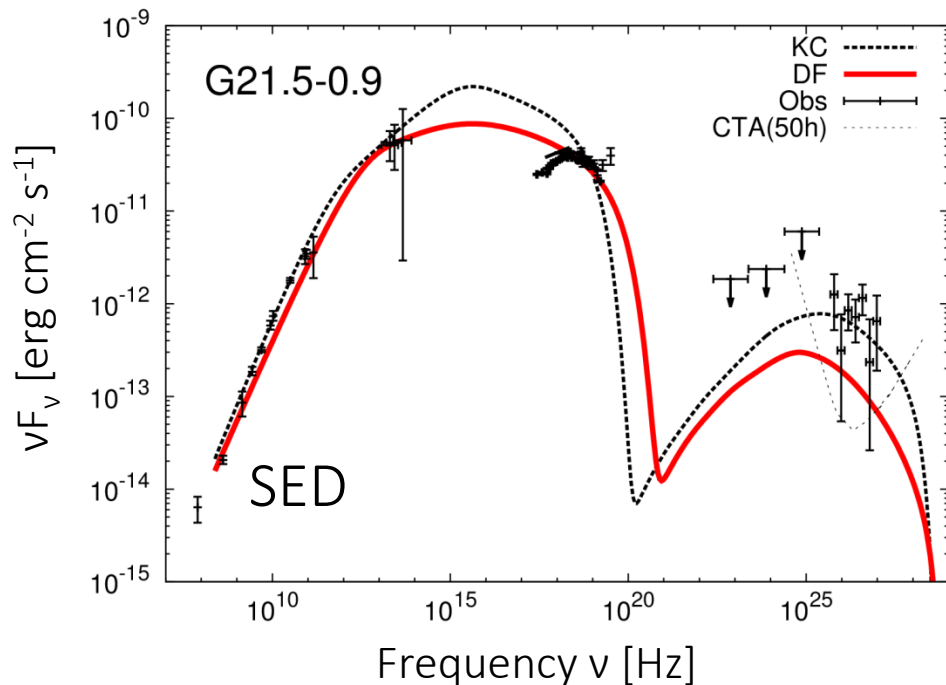
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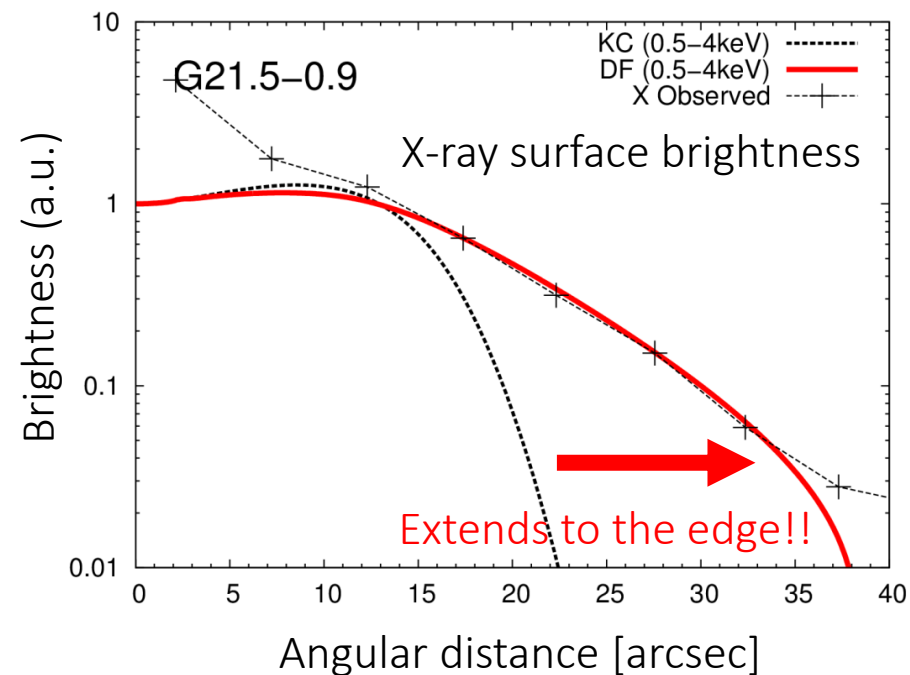
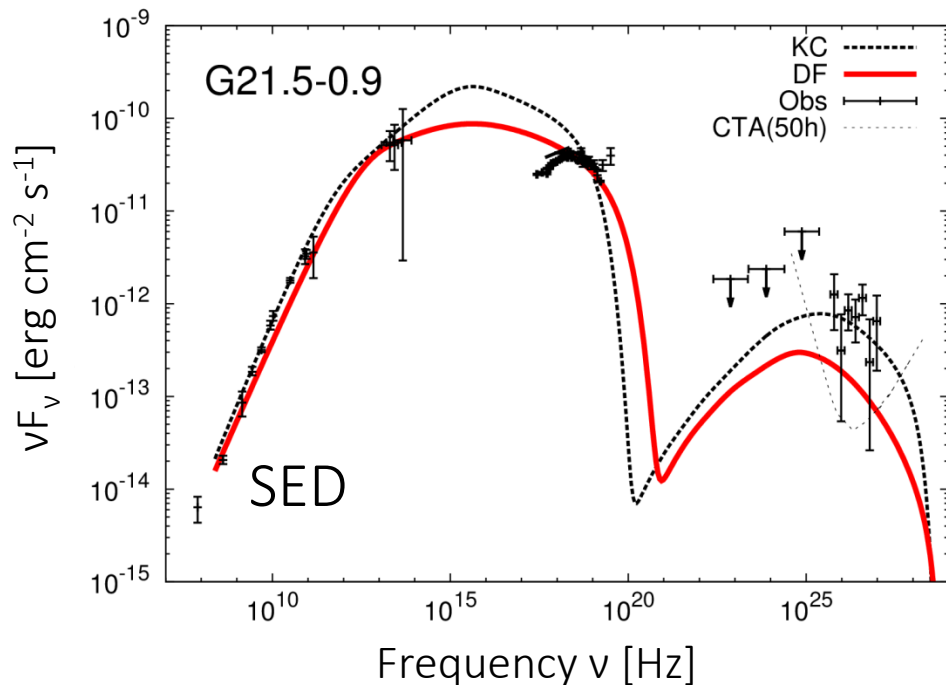
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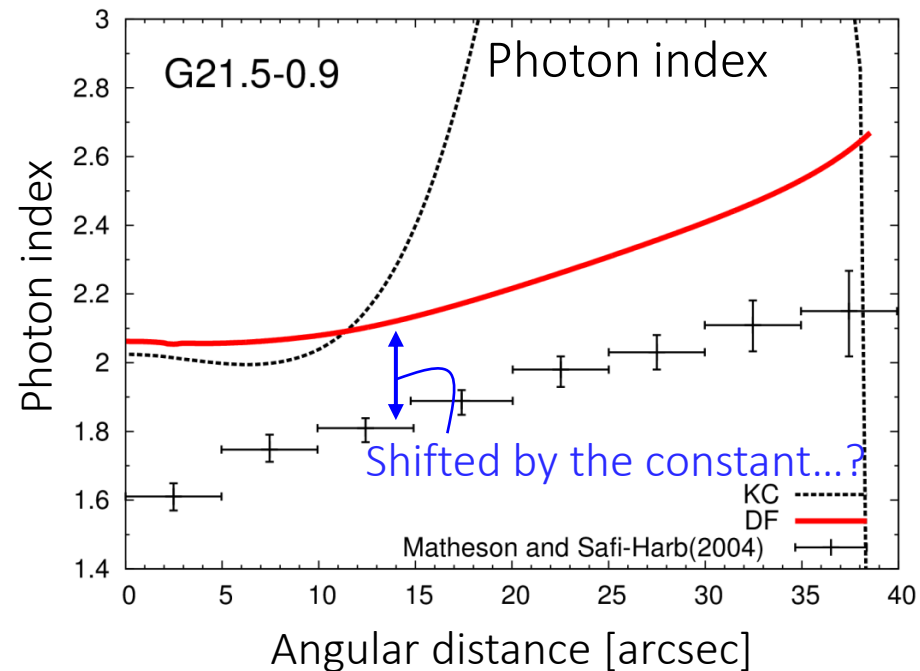
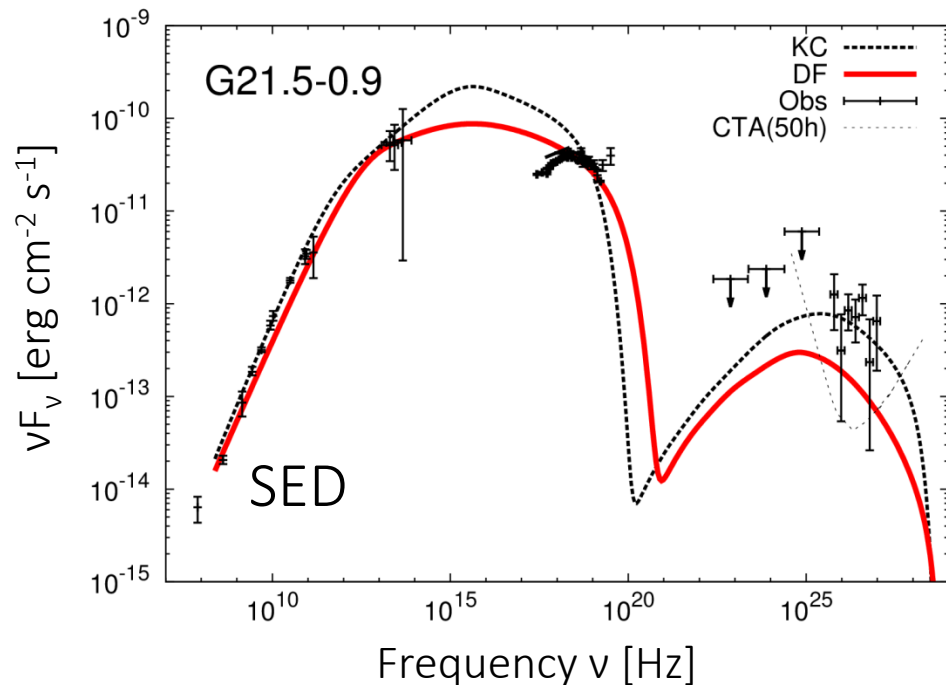
- Result for G21.5-0.9 (continues)

Photon index : The problematic softening is **solved**.

The radial dependence is in **good agreement**.

However it **is shifted by the constant** systematically.

SED: flux around 1 TeV is about **2 times** ($10^{-13} \text{ erg cm}^{-2} \text{ s}^{-1}$) insufficient as observed value.



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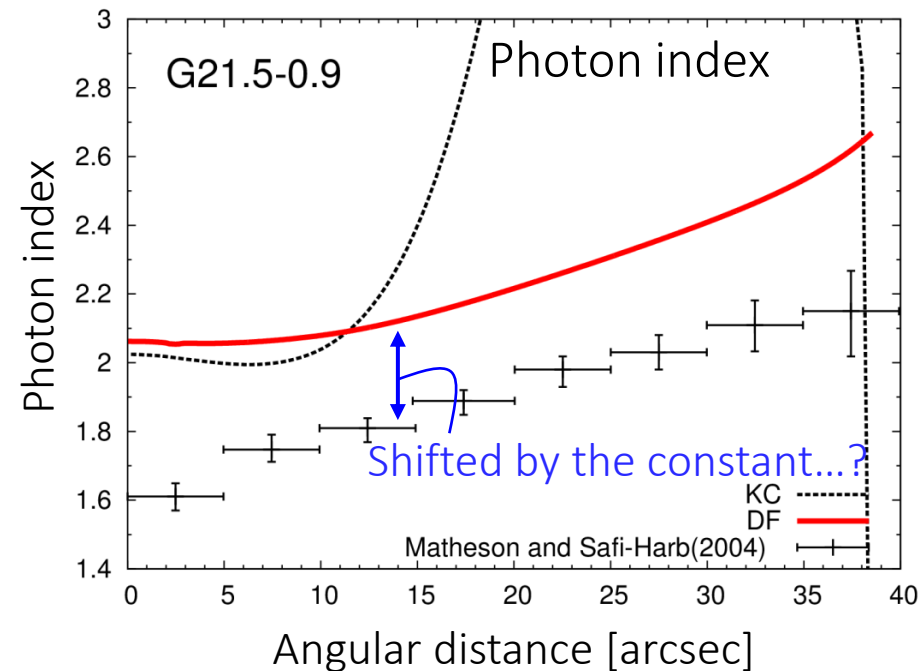
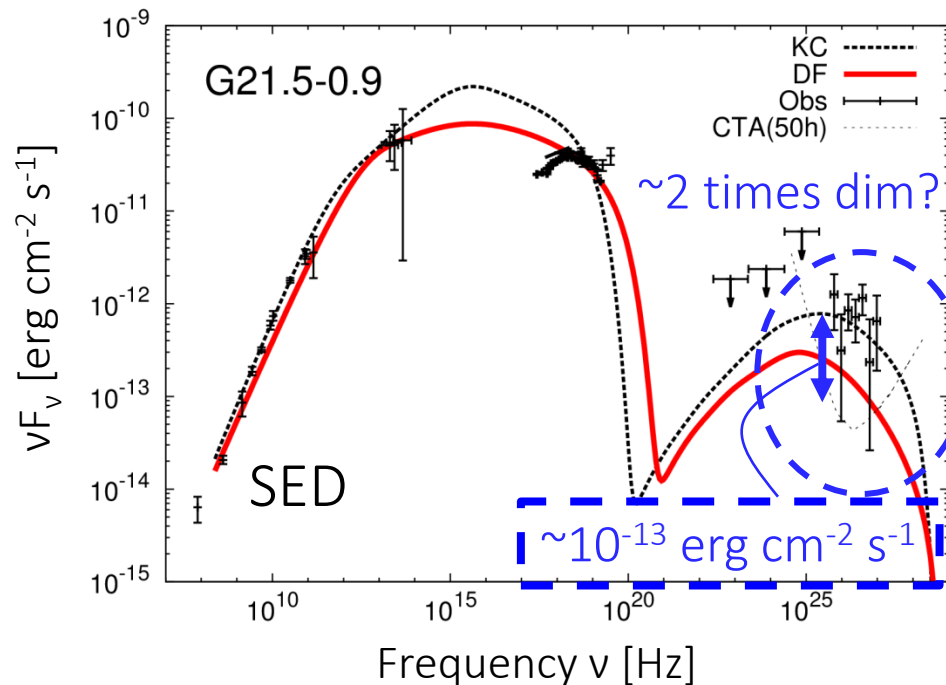
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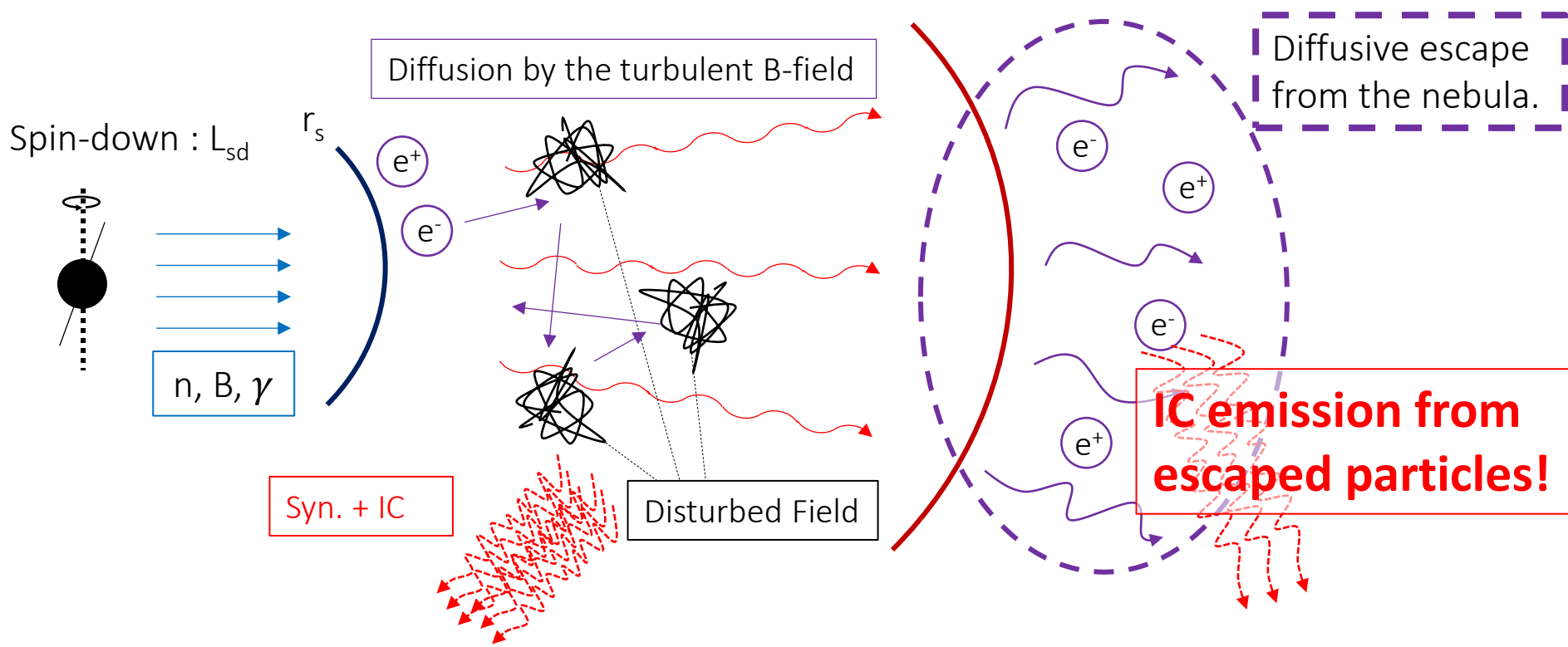


Escaped particles...?

- The γ -ray emission from the particles which escaped out of the nebula.
→ predict a “**young TeV-halo**” which extends larger than the radio or X-ray nebula.

Contribution from the escaped particles : $\sim 10^{-13} \text{ erg cm}^{-2} \text{ s}^{-1}$ → CAN cover the shortfall.

Assuming that the diffusion coefficient outside the nebula is same as inside one,
the extent of the γ -ray halo is $\sim 2 \text{ pc}$ (corresponding to $90''$)



Conclusion

- Summary :
 - ✗ The standard 1D steady model (KC model) CANNOT explain observation facts of PWNe where X-rays extends to the same as radio nebula.
 - ✿ We have shown that the SED and the extent of X-ray can be reproduces simultaneously by the 1-D steady diffusion model.
 - Assuming that the diffusion coefficient outside the nebula is the same as in the nebula, we have suggest that the “young TeV-halo” extends larger than the radio or X-ray nebula.
- Future prospects and issues :
 - A physical interpretation of the obtained diffusion coefficient $\kappa(E = 10^{14} \text{ eV}) \sim 10^{27} \text{ cm}^2 \text{ s}^{-1}$, which is much larger than the predicted value by the standard cosmic-ray diffusion model.
 - More quantitative modeling of the process of particle escaping from PWNe.
 - More objects.